



*Pseudo-scalar semileptonic  
analysis from FOCUS*

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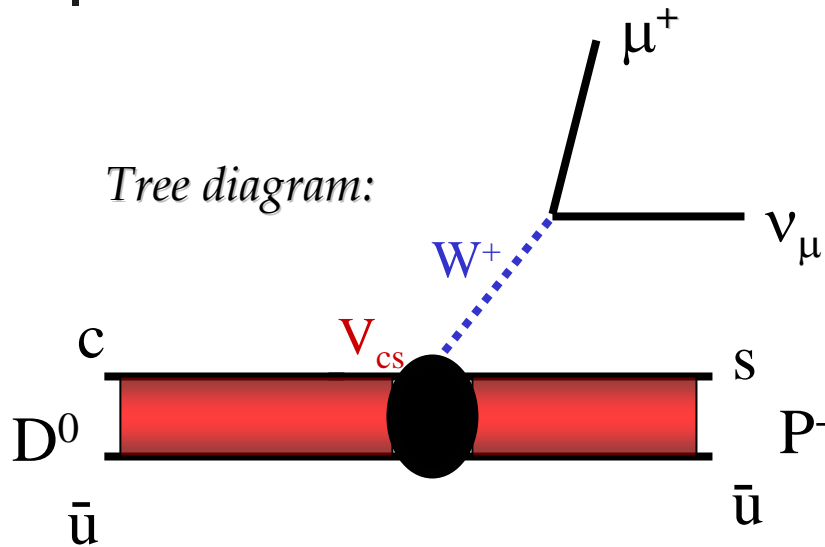


# Outline

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- ✓ *Pseudo-scalar semileptonic decays: why are they interesting?*
- ✓  *$D^0 \rightarrow \pi^- \mu^+ \nu$  and  $D^0 \rightarrow K^- \mu^+ \nu$  reconstruction in FOCUS.*
- ✓ *Parametric analysis:*
  - ✓ *Branching Ratio.*
  - ✓ *Pole Masses and  $f_{K^-}^K(0)/f_{K^+}^K(0)$ .*
  - ✓ *Form factor ratio  $f_{\pi^+}^{\pi}(0)/f_{K^+}^K(0)$*
- ✓ *Non parametric analysis of  $D^0 \rightarrow K^- \mu^+ \nu$   $q^2$ -dependence.*
- ✓ *Conclusions.*

# Pseudoscalar semileptonic decays



$$H \propto \frac{G_F}{\sqrt{2}} J_H^\mu \bar{\psi}_l \gamma_\mu (1 - \gamma_5) \psi_\nu$$

*Hadronic current contains information about strong contribution.  
 Parametrization of hadronic current is simple:*

The differential decay rate is:

$$J_H^\mu = f_+(q^2)(D + P)^\mu + f_-(q^2)(D - P)^\mu$$

$$\frac{d\Gamma(D \rightarrow P l \nu)}{dq^2} \propto |f_+(q^2)|^2 (A + B\eta + C\eta^2)$$

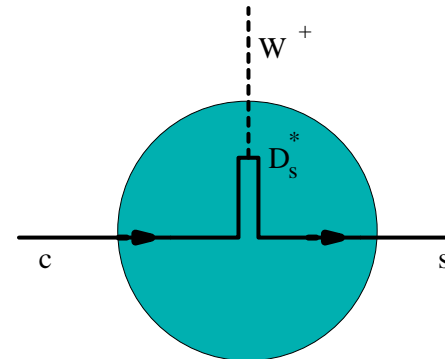
$$\eta = \frac{f_-(0)}{f_+(0)}$$

*Measuring the  $q^2$  dependence and the form factors in heavy to light quark transitions is critical to our understanding of QCD.*

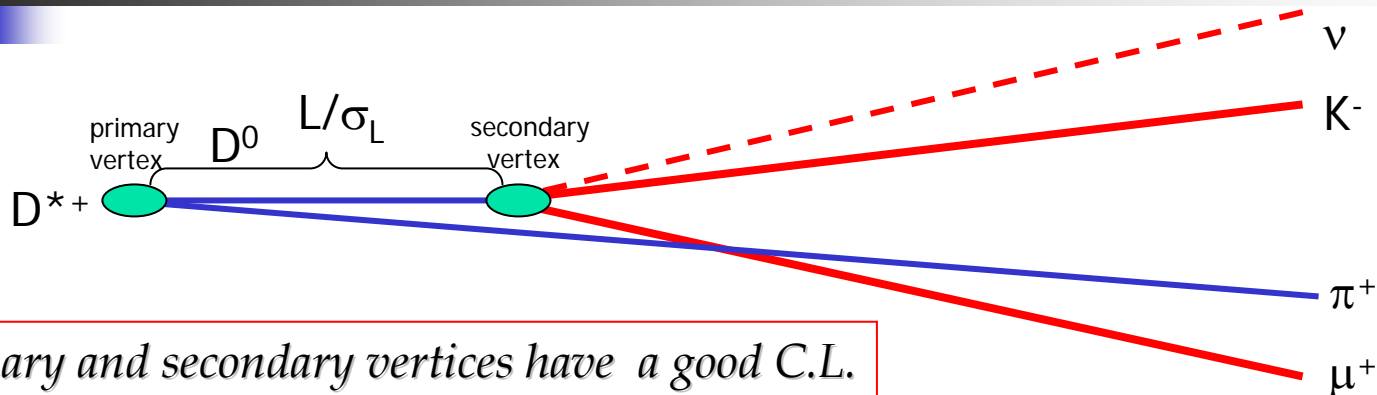
# What do we measure?

- $\pi\mu\nu$  to  $K\mu\nu$  branching ratio
- pole masses
- $f_-(0)/f_+(0)$ : contributions from  $f_-$  are still not measured since they are proportional to the lepton mass squared.
- $f_{\pi^+}(0)/f_{K^+}(0)$ : test of SU(3) symmetry breaking.
- non parametric  $q^2$  dependence: a model independent measurement would allow us to discriminate between different models.

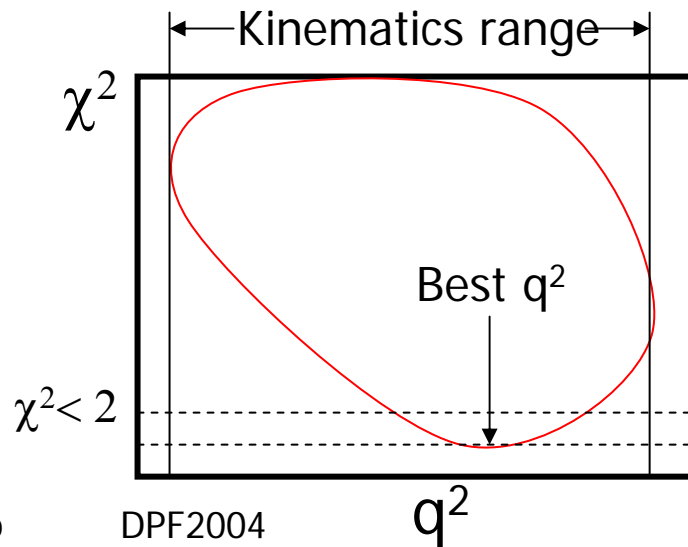
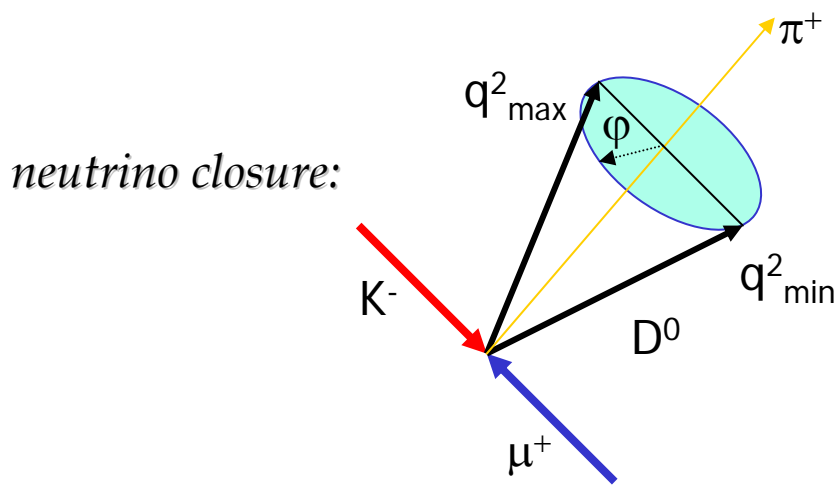
$$f_{\pm}(q^2) = \frac{f_{\pm}(0)}{1 - \frac{q^2}{M^2}}$$



# Semileptonic decay reconstruction



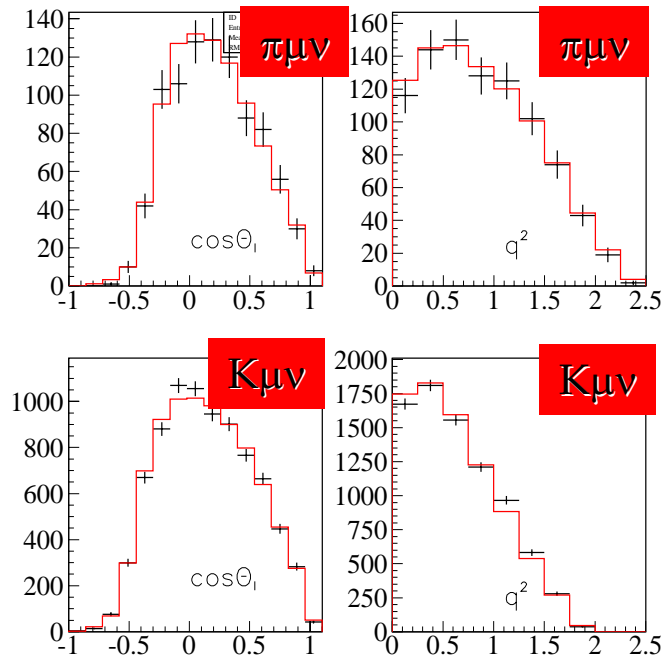
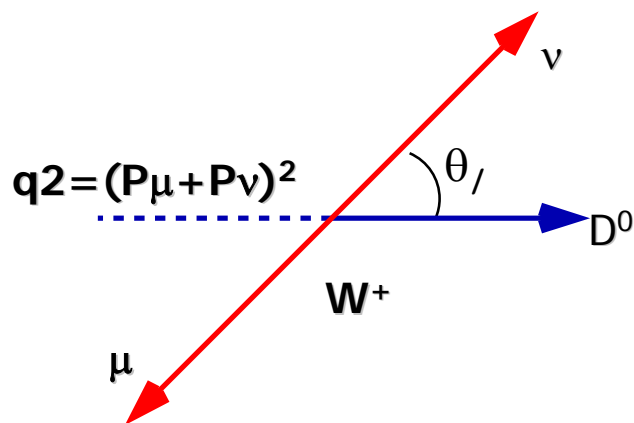
- primary and secondary vertices have a good C.L.
- Visible mass  $> 1.0 \text{ GeV}/c^2$
- $L/\sigma_L > 6$
- Cerenkov ID on K ( $\pi$ ) and soft pion



# Fitting technique

The fitting procedure consists of a fit to the  $K_{\mu\nu}$  sample and the subsequent use of this information to determine  $\pi_{\mu\nu}$  background.

- Fit to the  $D^*-D$  mass difference to find the amount of combinatoric background.
- Cut on the mass difference to suppress combinatoric and peaking background.
- Fit to  $\cos\theta_l$  and  $q^2$  to measure branching ratio, pole masses and the ratio  $f_-(0)/f_+(0)$ .



$$F = -2\ln(\pi_{\mu\nu}) + \chi_1^2 \quad \chi_1^2 = (BR_{(\rho^-/K^{*-})} - 0.080)^2 / (0.01)^2$$

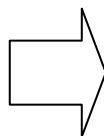
$$F = -2\ln(K_{\mu\nu}) + \chi_2^2 \quad \chi_2^2 = (BR_{(K^{*/}K)} - 0.63)^2 / (0.05)^2$$

# Weighting procedure

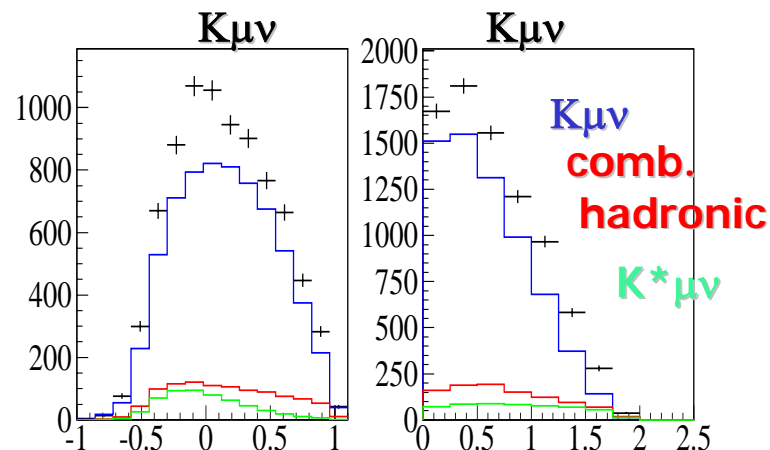
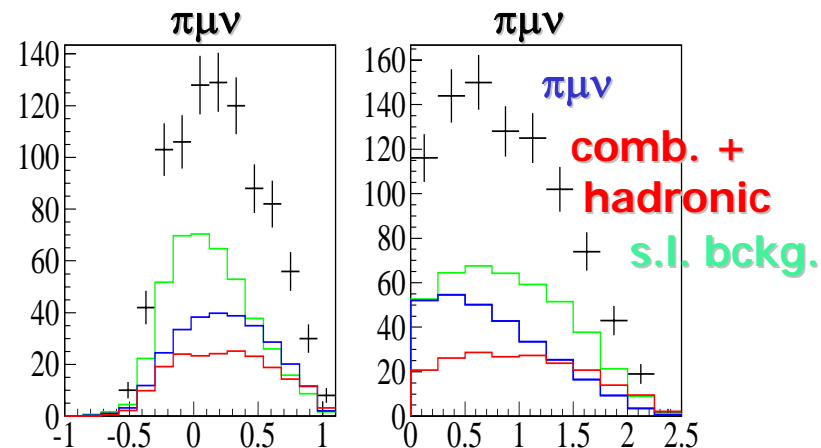
To measure pole masses and form factors we apply an event by event weighting:

$$\text{Weight} = \frac{I(m') / \text{Norm.}(m')}{I(m^0) / \text{Norm.}(m^0)}$$

where  $I \propto |f_+(q^2)|^2 g\left(\frac{f_-(0)}{f_+(0)}\right)$



$\pi\mu\nu$  and  $K\mu\nu$  shapes and efficiencies change during the fitting process.

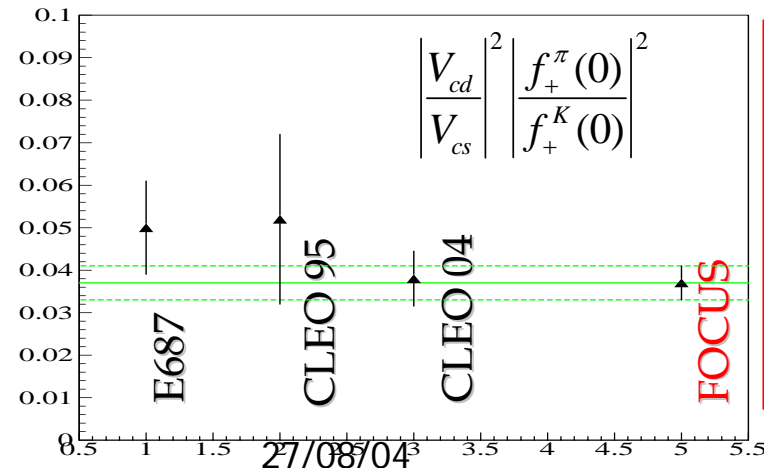
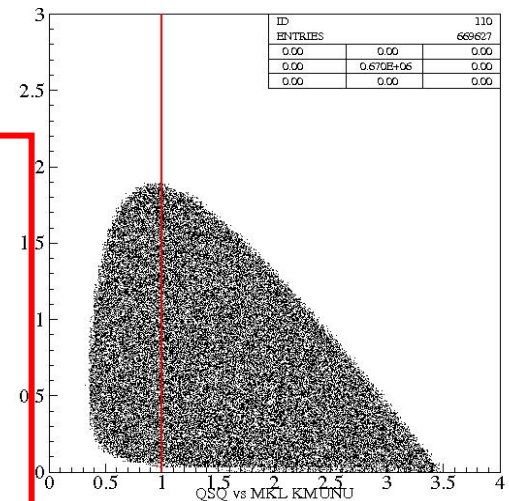
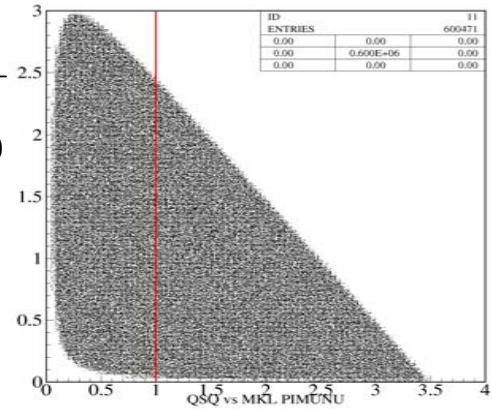


	Yield	B.R.(%)	Pole mass	$\frac{f_-^K(0)}{f_+^K(0)}$
$\pi\mu\nu$	$288 \pm 29$	$7.4 \pm 0.8$	$1.89^{+0.28}_{-0.14}$	
$K\mu\nu$	$6572 \pm 92$	100.	$1.92^{+0.05}_{-0.04}$	$-1.69^{+1.8}_{-1.5}$

# Extracting $f_+^\pi(0) / f_+^K(0)$

$$\frac{Y(\pi\mu\nu)}{Y(K\mu\nu)} = \left| \frac{f_+^{\pi\mu\nu}(0)}{f_+^{K\mu\nu}(0)} \right|^2 \left| \frac{V_{cd}}{V_{cs}} \right|^2 \frac{\int_{E_{l\min}}^{E_{l\max}} dE_l \int_{q^2_{\min}(E_l)}^{q^2_{\max}(E_l)} dq^2 \frac{f_+^{\pi\mu\nu}(q^2)}{f_+^{\pi\mu\nu}(0)} (A + B\eta + C\eta^2) \varepsilon^{\pi\mu\nu}(q^2)}{\int_{E_{l\min}}^{E_{l\max}} dE_l \int_{q^2_{\min}(E_l)}^{q^2_{\max}(E_l)} dq^2 \frac{f_+^{K\mu\nu}(q^2)}{f_+^{K\mu\nu}(0)} (A + B\eta + C\eta^2) \varepsilon^{K\mu\nu}(q^2)}$$

- Yields from the fit
- Efficiency as a function of  $q^2$ .
- $|V_{cd}/V_{cs}|^2 = 0.051$
- Compute a numerical integration on the Dalitz.



$$\left| \frac{V_{cd}}{V_{cs}} \right|^2 \left| \frac{f_+^\pi(0)}{f_+^K(0)} \right|^2 = 0.037 \pm 0.04$$

$$\frac{f_+^\pi(0)}{f_+^K(0)} = 0.85 \pm 0.04(stat.)$$

# Systematic studies and results

- Fit fluctuated data to test for biases and errors.
- Fit fluctuated fit function to test goodness of fit.
- Cut variations to verify Monte Carlo simulation.
- High statistics  $D^+$  and  $D^0$  decays used to test K to pi misidentification rate.
- Fit variations and alternative fitting procedure.
- Variations on the amount of backgrounds.
- Test on weak constraints increasing the input error by a factor of 10.

$$\frac{\Gamma(\pi^- \mu^+ \nu)}{\Gamma(K^- \mu^+ \nu)} = 0.074 \pm 0.008(stat.) \pm 0.006(sys.)$$

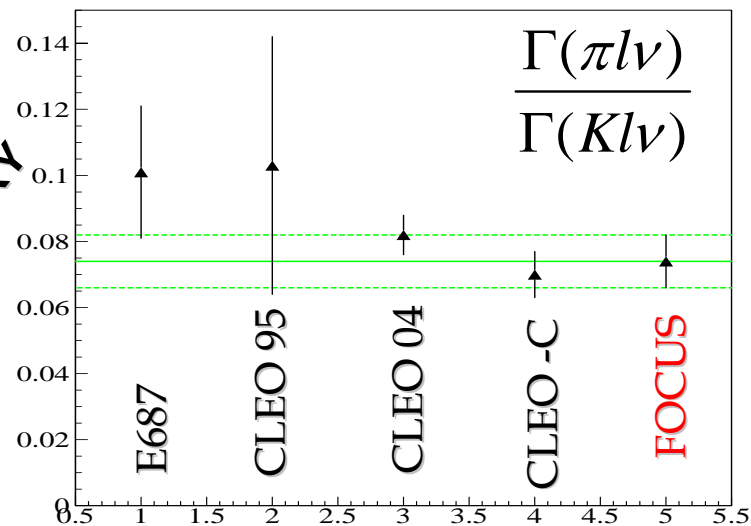
$$M_\pi = 1.89_{-0.14}^{+0.28} (stat.) \pm 0.07(sys.)$$

$$M_K = 1.92_{-0.04}^{+0.05} (stat.) \pm 0.03(sys.)$$

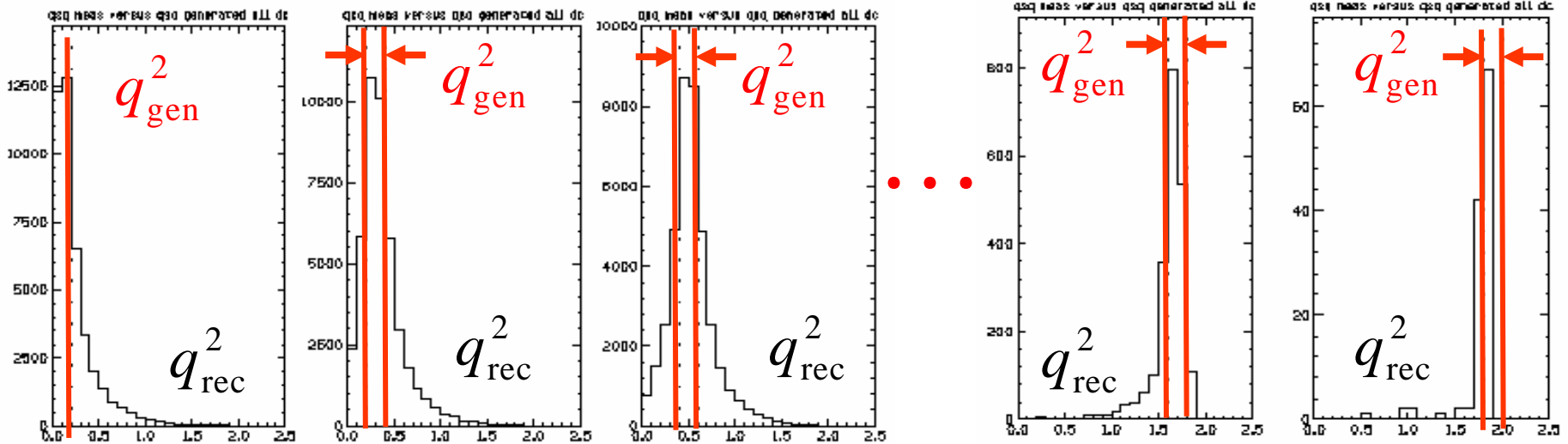
$$\frac{f_-^K(0)}{f_+^K(0)} = -1.69_{-1.5}^{+1.8} (stat.) \pm 0.3(sys.)$$

$$\frac{f_+^\pi(0)}{f_+^K(0)} = 0.85 \pm 0.04(stat.) \pm 0.04(sys.)$$

PRELIMINARY



# Correcting for smearing in FOCUS

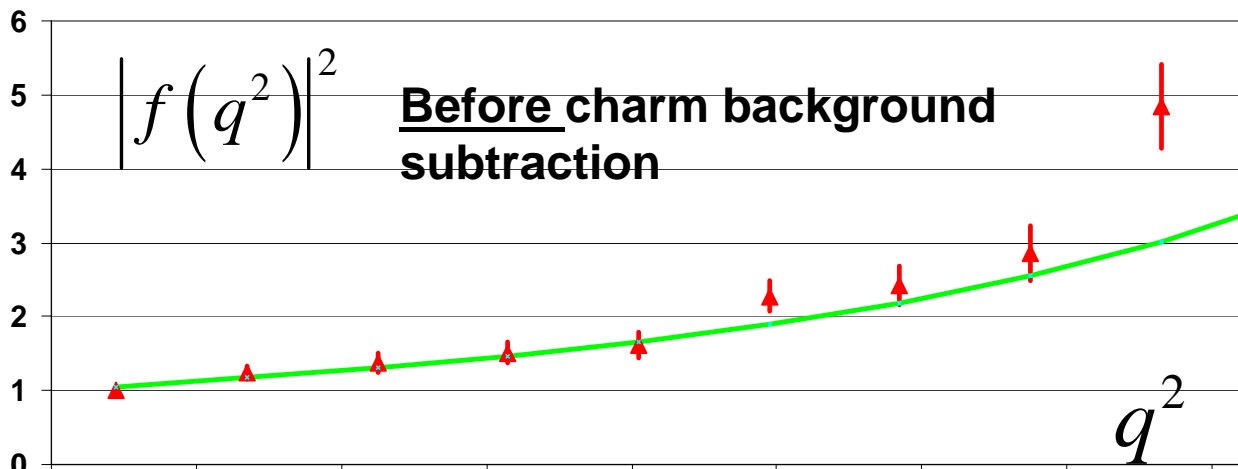


A deconvolution matrix is constructed from the number of events generated in the  $i$ -th  $q^2$  bin that end up reconstructed in the  $j$ -th  $q^2$  bin. This matrix is then used to correct data for resolution and efficiency

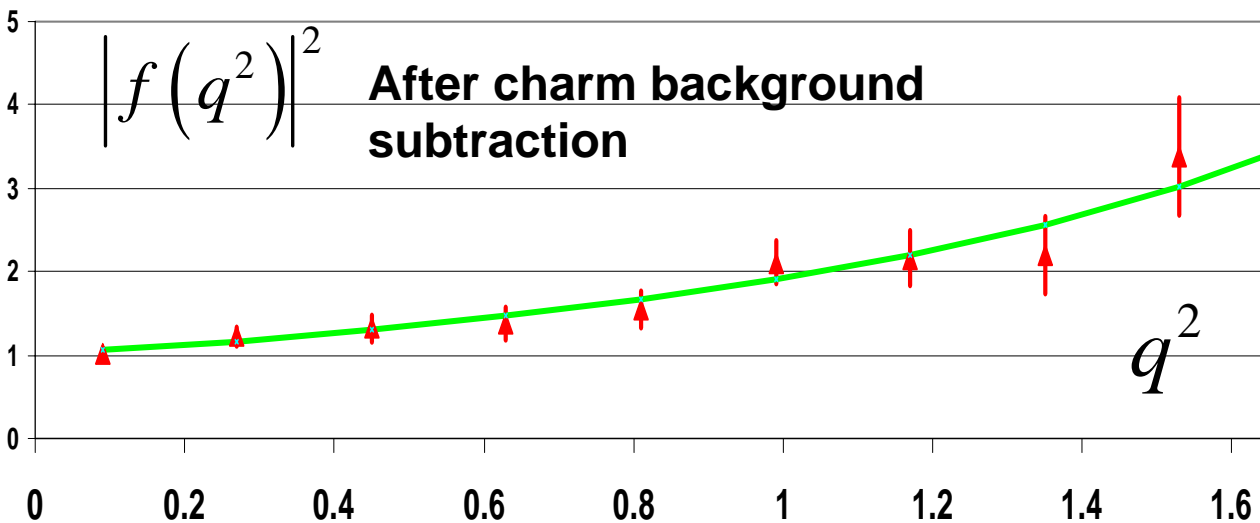
$$\begin{pmatrix} N_{M1}^{G1} / \tilde{f}_1^2 & N_{M1}^{G2} / \tilde{f}_2^2 & N_{M1}^{G3} / \tilde{f}_3^2 \\ N_{M2}^{G1} / \tilde{f}_1^2 & N_{M2}^{G2} / \tilde{f}_2^2 & N_{M2}^{G3} / \tilde{f}_3^2 \\ N_{M3}^{G1} / \tilde{f}_1^2 & N_{M3}^{G2} / \tilde{f}_2^2 & N_{M3}^{G3} / \tilde{f}_3^2 \end{pmatrix}^{-1} \begin{pmatrix} \tilde{M}_1 \\ \tilde{M}_2 \\ \tilde{M}_3 \end{pmatrix} = \begin{pmatrix} f^2(q_1^2) \\ f^2(q_2^2) \\ f^2(q_3^2) \end{pmatrix}$$

**We actually use a  $10 \times 10$  matrix**

# Correcting for charm backgrounds

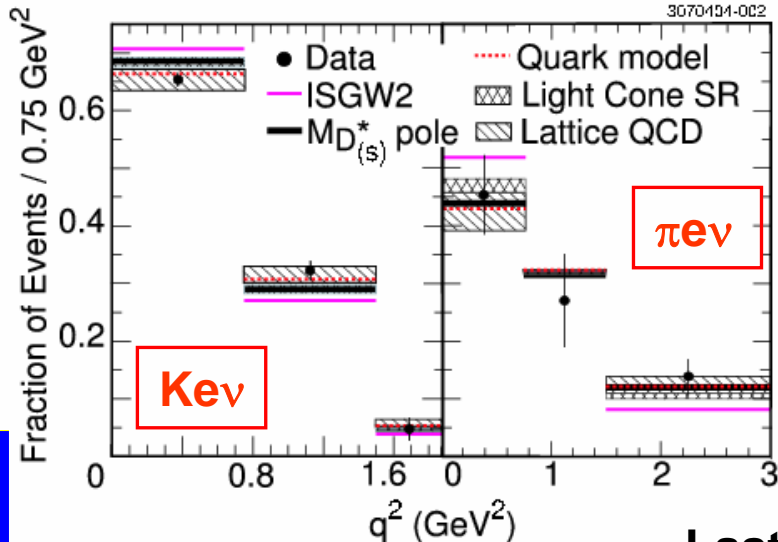
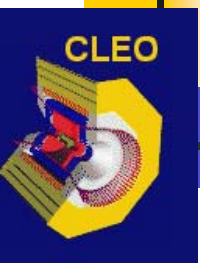


Interestingly enough the backgrounds seem to be primarily at high  $q^2$



After subtracting known charm backgrounds  $f_+(q^2)$  is an excellent match to a pole form with  $m_{\text{pole}} = 1.92 \text{ GeV}$

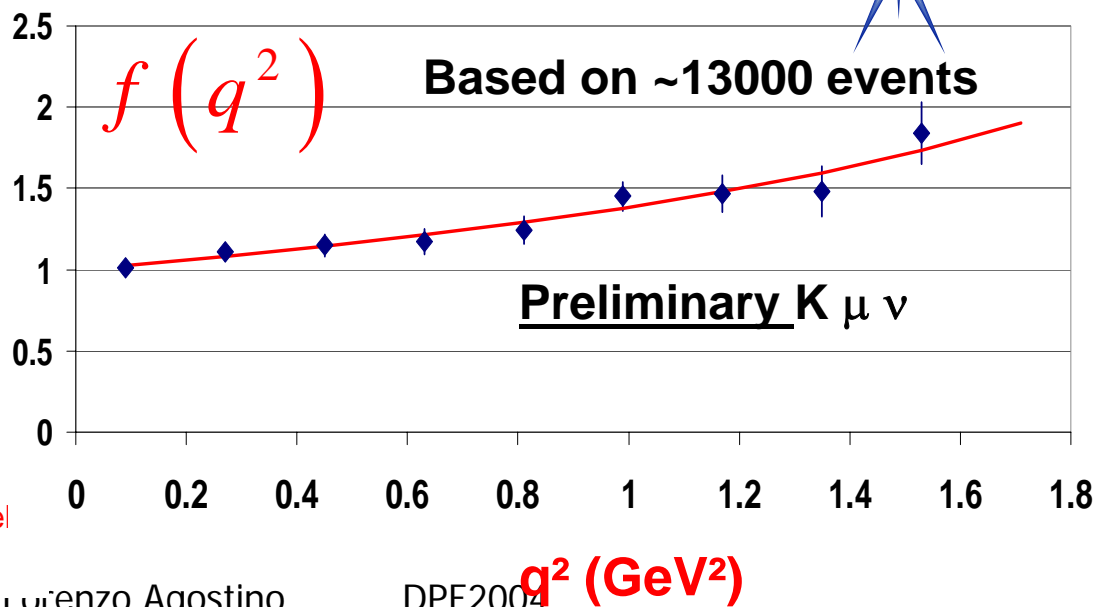
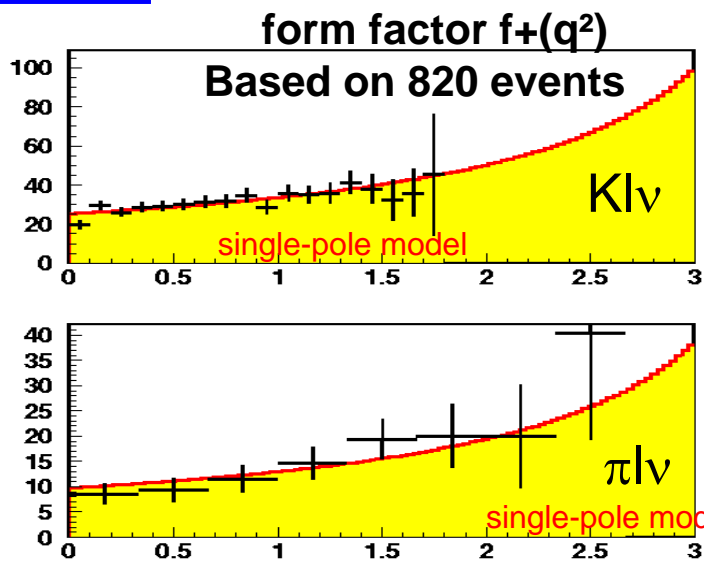
# How do we compare on $f_+(q^2)$ ?



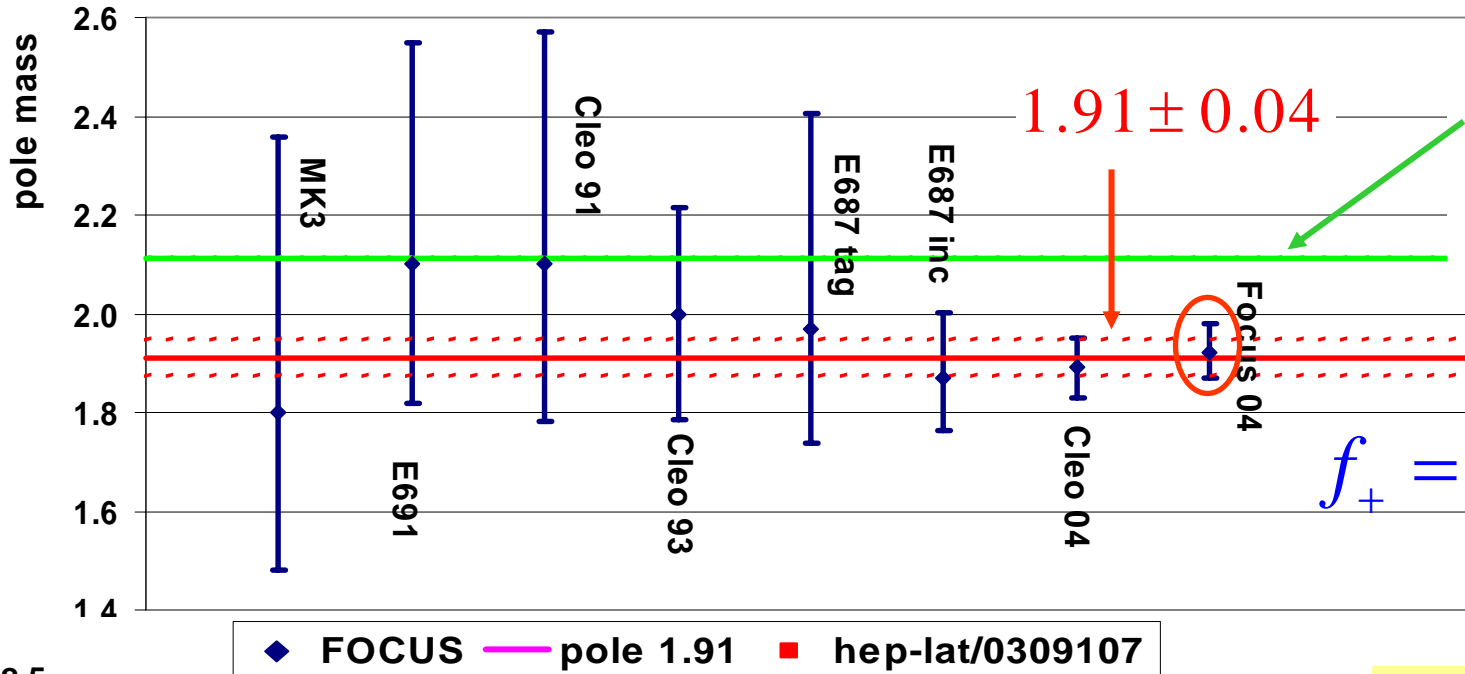
Three (!) brand new results from CLEO, BELLE, and FOCUS on  $f_+(q^2)$



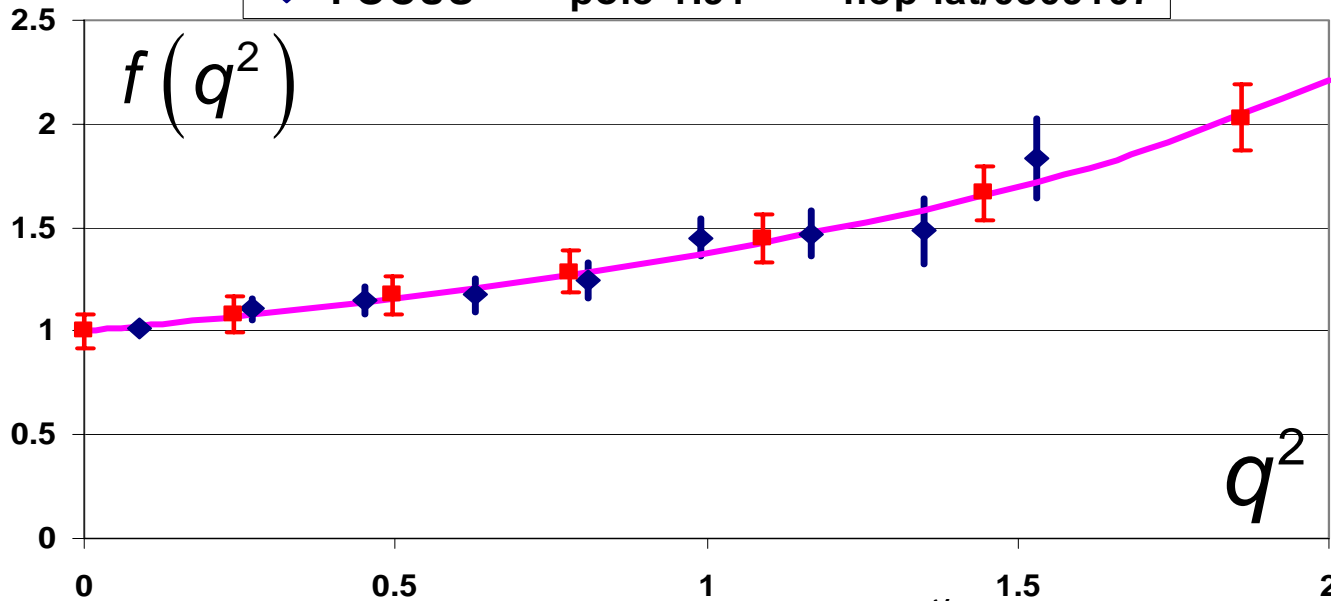
Last but not least....



# Pole mass fits and LQCD calculations



$$f_+ = \frac{f_+(0)}{1 - q^2 / m_{\text{pole}}^2}$$



Agreement with LQCD unquenched calculation is also very impressive!

This calculation predicts  $f_+^{\pi}(0)/f_+^K(0)=0.85$  in great agreement with the FOCUS result.

## Conclusions

- *We presented new results on  $D^0$  pseudoscalar semileptonic decays from FOCUS. We measured the pole masses for both  $\pi\mu\nu$  and  $K\mu\nu$ , the form factor ratio  $f_-^K(0)/f_+^K(0)$  as well as the ratio  $f_+^\pi(0)/f_+^K(0)$ .*
- *The pole masses are lower than the predicted values at the  $D^*$  or  $D_s^*$  masses.*
- *We have the best measurement of  $f_+^\pi(0)/f_+^K(0)$  which is consistent with the predictions from SU(3) symmetry breaking and lattice QCD.*
- *The  $\pi\mu\nu$  to  $K\mu\nu$  branching ratio is consistent with recent results from CLEO.*
- *Finally we presented a non-parametric analysis of the  $q^2$  dependence for  $D^0 \rightarrow K\mu\nu$  which shows excellent agreement with the results obtained with the parametric analysis and Lattice QCD.*