

$B^- \rightarrow D^0(K_s \pi^+ \pi^-)K^-$ dalitz fit

Measurement of CKM angle γ via dalitz technique

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On behalf of BaBar Collaboration

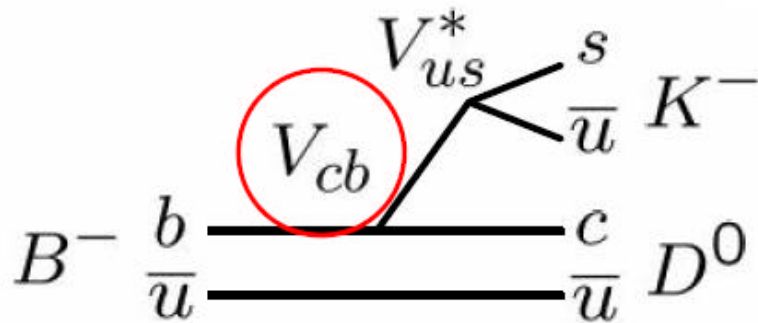
Outline:

1. Description of the method
2. Events selection
3. Background fighting
4. The D^0 dalitz model
5. Statistics and Systematic error.

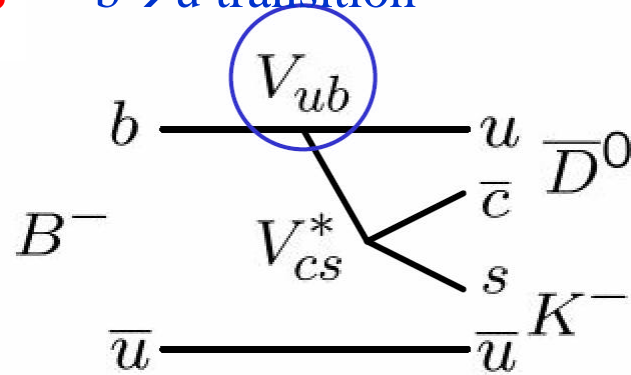


DPF 2004, UC Riverside, August 26-31, 2004



Probe CKM g via $B^- \rightarrow D^0 K^-$ channel $b \rightarrow c$ transition

$$e^{i\delta_B} e^{-i\phi}$$

 $b \rightarrow u$ transitionInterference occur when D^0 and \bar{D}^0 decay to same final stateRelative size (r_B) of B decay amplitudes

Not well constrained by theory.

Larger r_B , larger interference, better g experimental precision

$$r_B = \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|$$

Work was pioneered by Belle hep-ex/0406067 $r_B = 0.26_{-0.14}^{+0.10} \pm 0.03 \pm 0.04$

$$m_+^2 : M(K_S \pi_+)^2$$

$$m_-^2 : M(K_S \pi_-)^2$$

Looking interference on dalitz plot

B₊: pdf = $| f(m_+^2, m_-^2) + r_b e^{i(\gamma+\delta)} f(m_-^2, m_+^2) |^2$ Weak phase change sign
Strong phase does not.

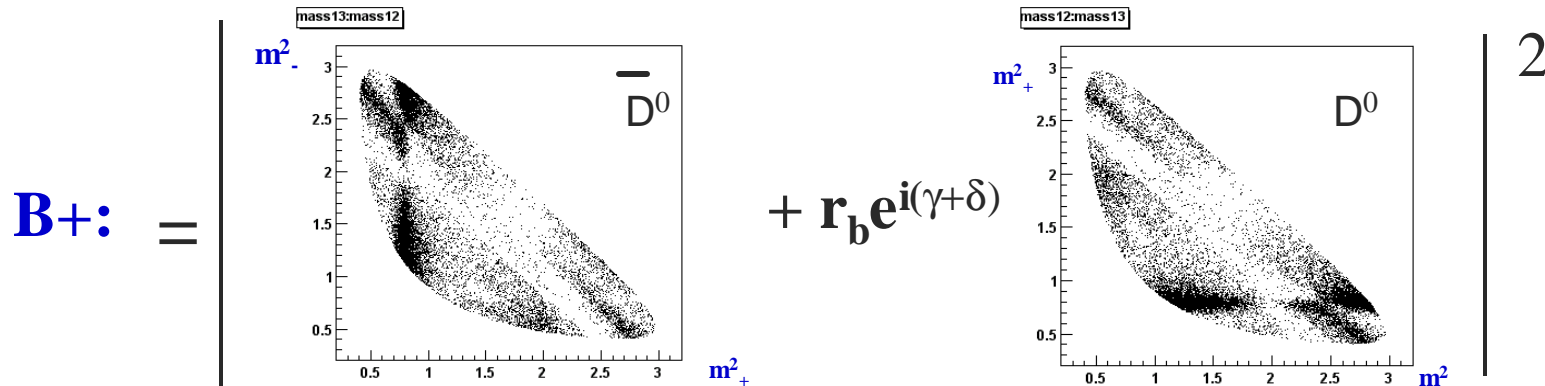
B₋: pdf = $| f(m_-^2, m_+^2) + r_b e^{i(-\gamma+\delta)} f(m_+^2, m_-^2) |^2$ D⁰ dalitz amplitude

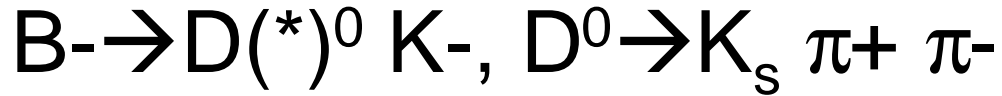
Fit B₊ → give r_b and θ₊ = γ + δ

Fit B₋ → give r_b and θ₋ = -γ + δ

We have → $\gamma = (\theta_+ - \theta_-) / 2$

Pictorially:





Candidate selections

- $K_s \rightarrow \pi^+ \pi^-$: $|m(K_s) - \text{PDG}| < 9 \text{ MeV}$
- $D^0 \rightarrow K_s \pi^+ \pi^-$: $|m(D^0) - \text{PDG}| < 12 \text{ MeV}$
- Bachelor Kaon: separate Kaons and Pions from DIRC

D^{*0} Candidate selections

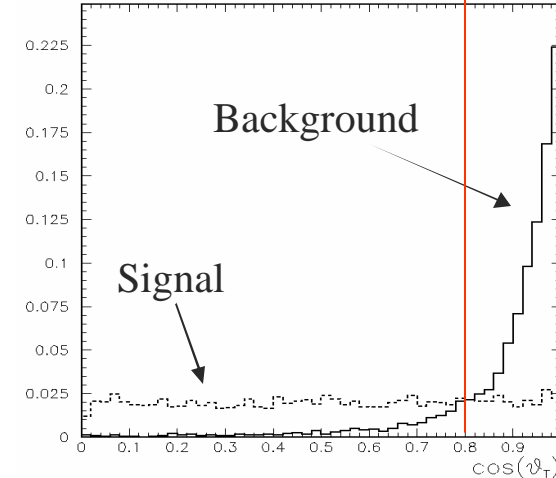
- Select γ, π^0 from the Electromagnetic Calorimeter
- $|\Delta m - \Delta m(\text{PDG})| < 2.5 \text{ MeV}$ in $D^0 \pi^0$ and $< 10 \text{ MeV}$ in the $D^0 \gamma$ mode

Δm : mass difference
between $D^* - D^0$

Background suppression:

- $|\text{Cos}(\theta_T)| < 0.8$ suppress jet-like qq background
- $|\Delta E| < 30 \text{ MeV}$ suppress the BB-component
- Legendre Fisher to further suppressed qq background.
- $\text{Cos}(\alpha_{K_s}) < 0.99$ suppressed fake K_s

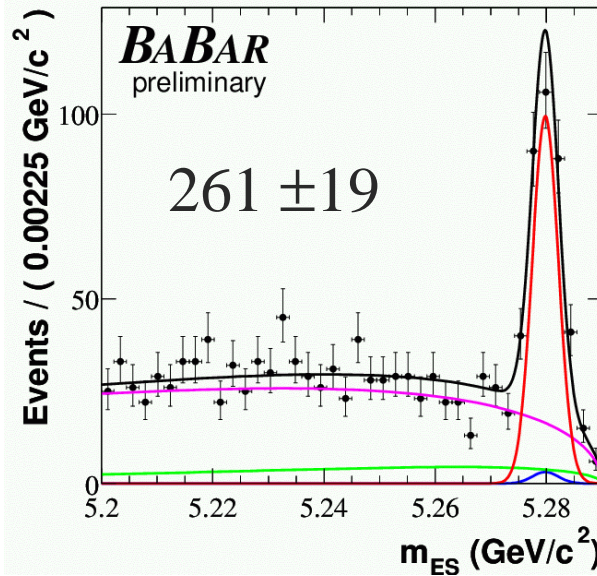
α_{K_s} : angle between K_s flight length and its momentum vector



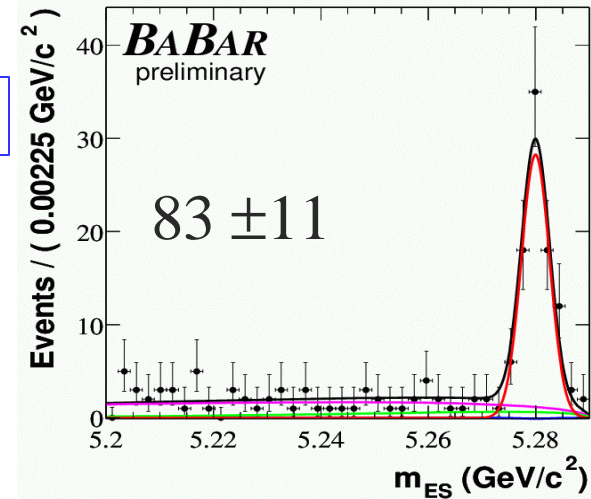
211 Millions $B\bar{B}$ pairs

Events selections

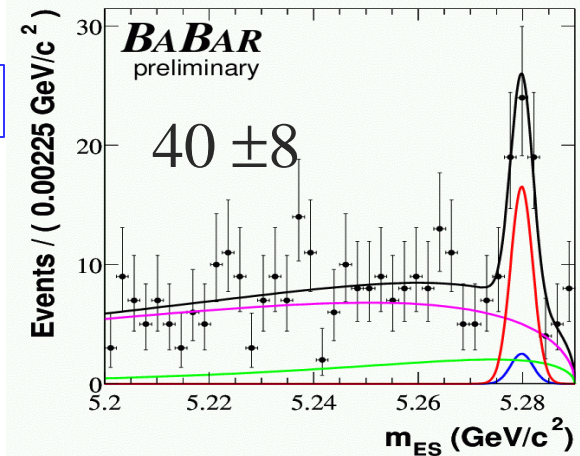
D^0K



$D^{*0}(D^0\pi^0)K$



$D^{*0}(D^0\gamma)K$



Legend:

- Black: Total pdf
- Red: Signal events
- Pink: udsc background events
- Green: BB background events
- Blue: $D\pi$ background events

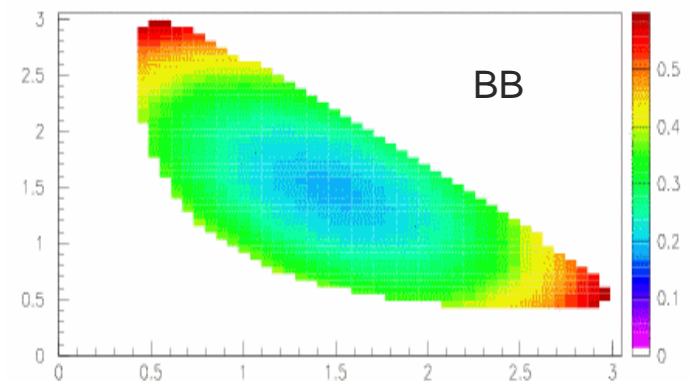
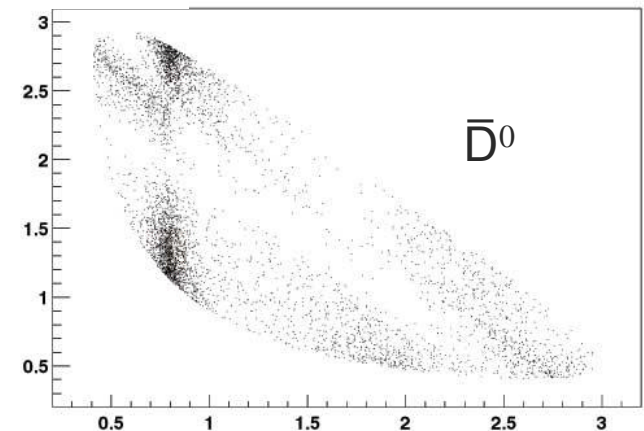
Source of Background I

In the dalitz plot analysis, one need:

- a.) The fraction of the background
- b.) The dalitz plot shapes

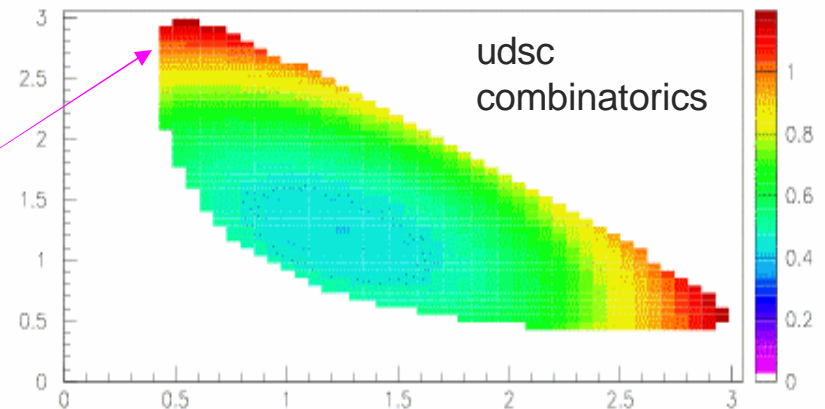
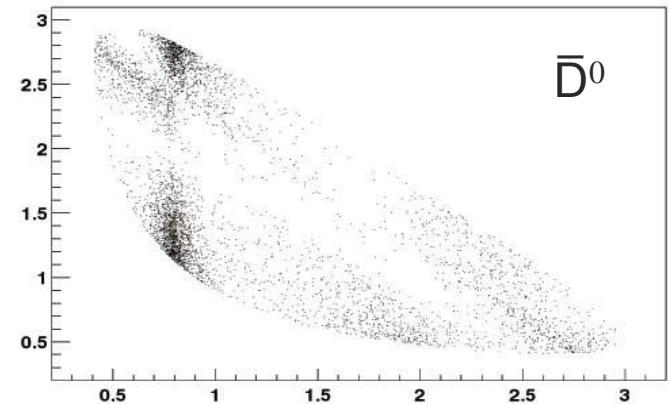
- $B \rightarrow D^0 \pi$ (~6%)
 - Shapes: From D dalitz model

- Generic B^+ / B^0 background (~5%)
 - Shapes: From Generic BB Monte Carlo



Source of background II

- udsc background(~26%)
 - In this background there are 21% are real $D^0 \rightarrow K_s \pi^+ \pi^-$ candidate, so need to separate:
 - Real D^0 candidate(21%): D^0 dalitz model
 - Fake D^0 candidate(Combinatorics)(79%): Shapes: from Off-resonance sample

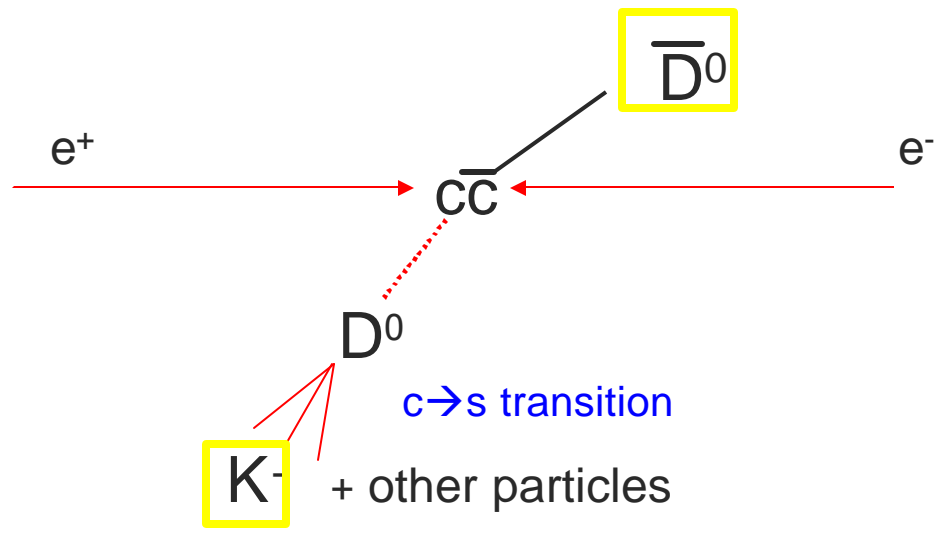


Notice in the combinatorics the dalitz distribution is not flat, it was due to the soft π and the events are more often pile up at the corner of the dalitz plot.

Understand background III:

Suppose want to select $B^- \rightarrow D^0 K^-$

More often in cc bkg, we select as $B^- \rightarrow \bar{D}^0 K^-$



V_{ub} like contribution

Flavor tagging not correct

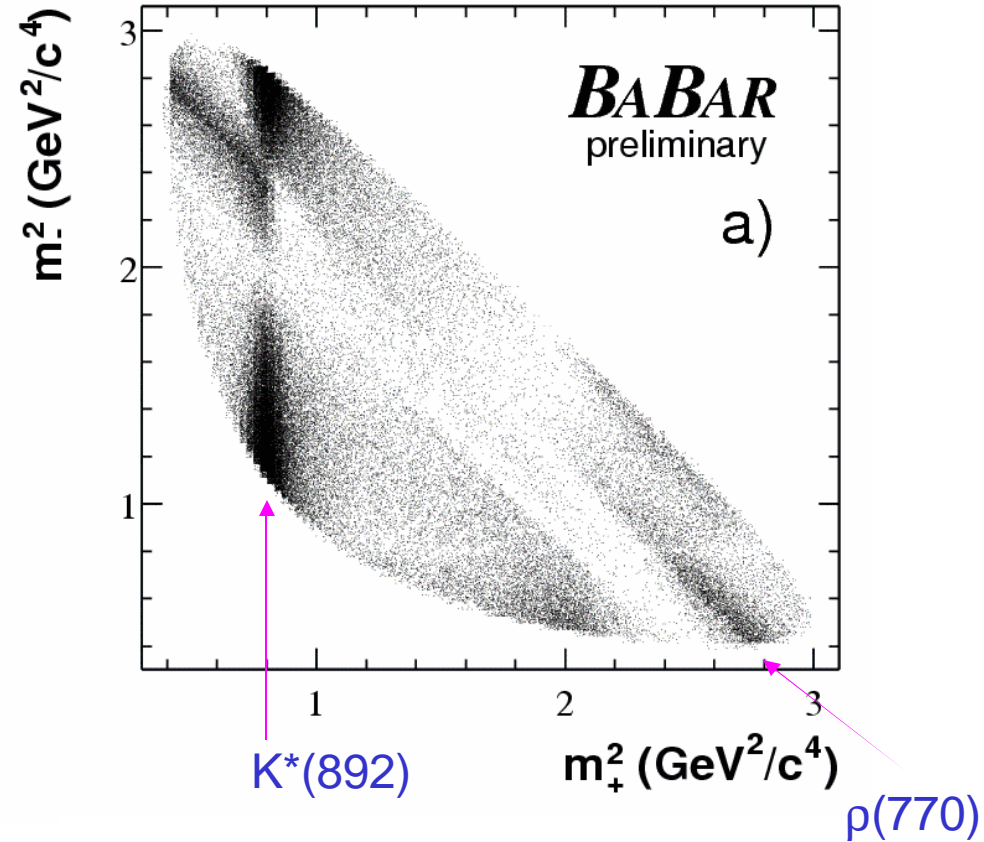
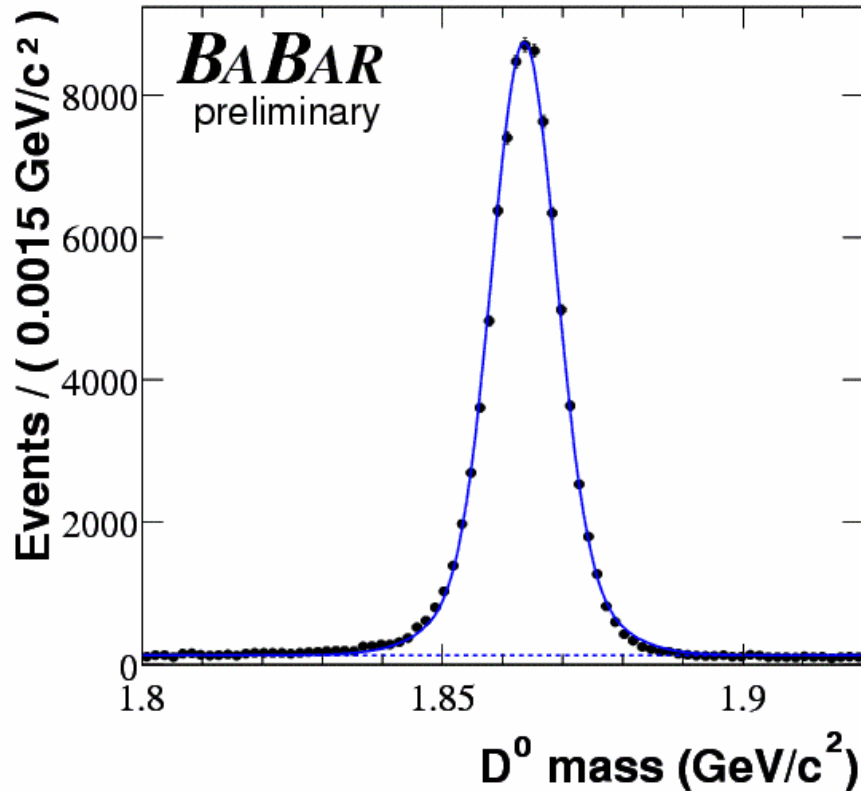
The wrong tagging rate is 79.2% (estimated from MC)

If one neglect this charge correlation effect, the r_b is biased.

From the toy MC study, neglecting this effect leads to a **+0.02** bias on r_b

Determined on $D^* \rightarrow D^0 \pi$ sample

The D^0 dalitz plot



Purity is 97%

81496 events selected using 91.5 fb⁻¹ data using $D^* \rightarrow D^0 \pi$ sample

[The dalitz (Isobar) model]

- We assumed the D^0 amplitude is represented by a sum of 2-body decay amplitude + non-resonant component (**Isobar model**)

Mathematically:

$$\sum_j a_j e^{iq_j} \times^J M_r \times BW^r + a_0 e^{iq_0}$$

--Angular Dependence
(spin 0,1,2)

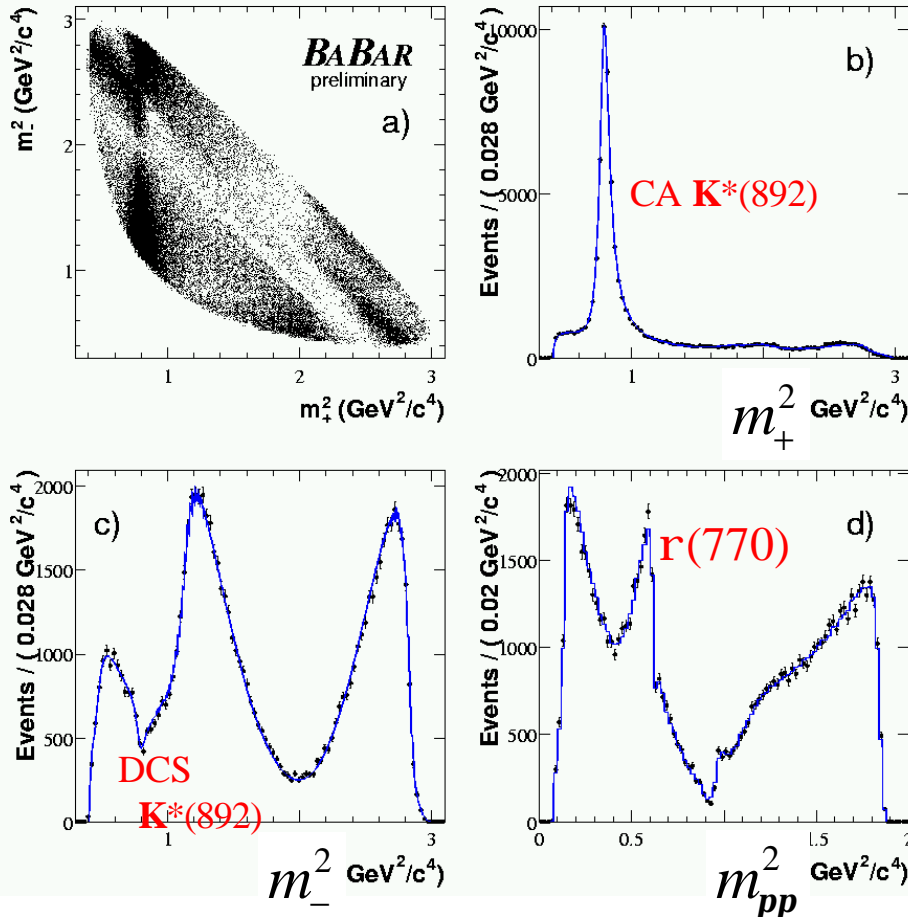
--Relativistic Breit-Wigner Form Factor
(the resonance!)¹

Non-resonance term

1. For $\rho(770)$ and $\rho(1450)$ we adopt Gounaris-Sakurai parameterization, see the mini-review on PDG

Determined on $D^ \text{ @ } D^0 p$ sample*

The dalitz model fit

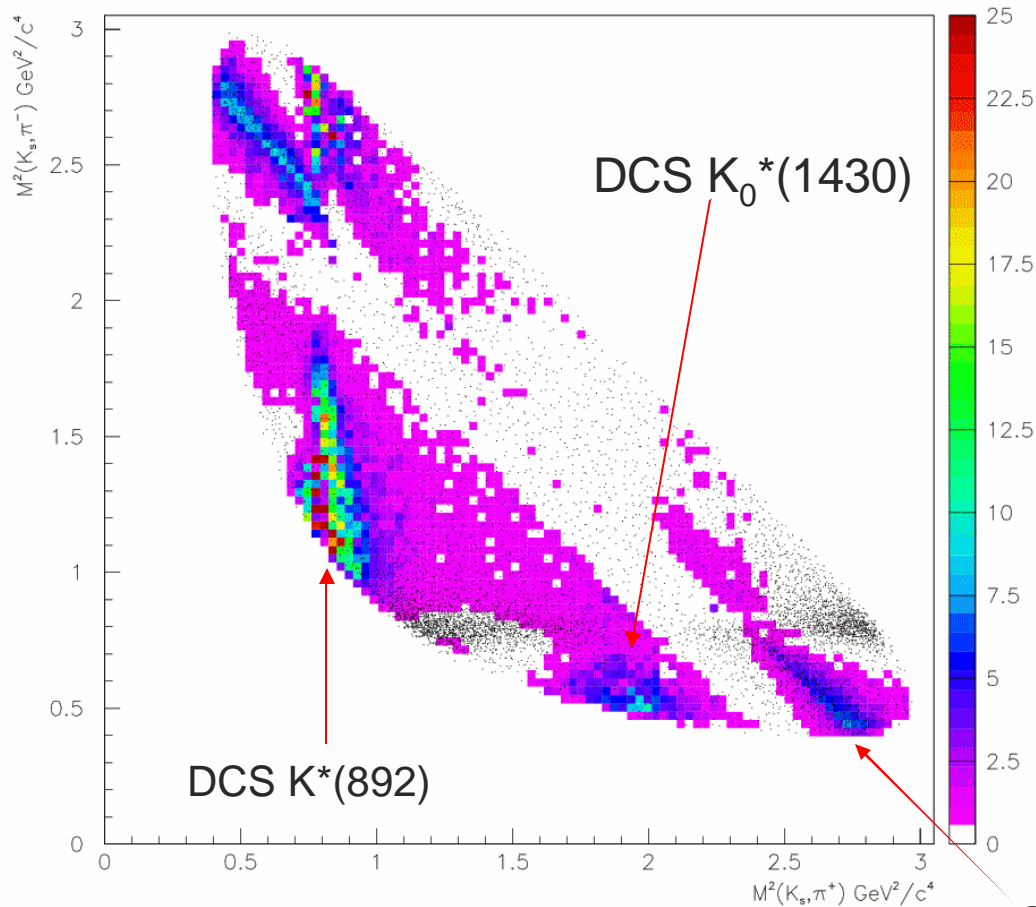


Resonance	Amplitude	Phase (degrees)	Fraction (%)
$K^*(892)$	1.777 ± 0.018	131.0 ± 0.81	58.51
$\rho^0(770)$	1 (fixed)	0(fixed)	22.33
$K^*(892)$ DCS	0.1789 ± 0.0080	-44.0 ± 2.4	0.59
$\omega(782)$	0.0391 ± 0.0016	114.8 ± 2.5	0.56
$f_0(980)$	0.469 ± 0.011	213.4 ± 2.2	5.81
$f_0(1370)$	2.32 ± 0.31	114.1 ± 4.4	3.39
$f_2(1270)$	0.915 ± 0.041	-22.0 ± 2.9	2.95
$K_0^*(1430)$	2.454 ± 0.074	-7.9 ± 2.0	8.37
$K_0^*(1430)$ DCS	0.350 ± 0.069	$-344. \pm 10.$	0.60
$K_2^*(1430)$	1.045 ± 0.045	-53.1 ± 2.6	2.70
$K_2^*(1430)$ DCS	0.074 ± 0.038	-98 ± 30	0.01
$K^*(1410)$	0.524 ± 0.073	-157 ± 10	0.39
$K^*(1680)$	0.99 ± 0.31	-144 ± 18	0.35
$\rho(1450)$	0.554 ± 0.097	$35 \pm 12.$	0.28
σ_1	1.346 ± 0.044	-177.5 ± 2.5	9.11
σ_2	0.292 ± 0.025	-206.8 ± 4.3	0.98
Non resonant	3.41 ± 0.48	-233.9 ± 5.0	6.82

Total fit-Fraction is 124%

13 resonances + 3 DCS partner + 1 non resonant component

Which part of the dalitz plot is sensitive to γ ?



We computed the 2nd derivative of the likelihood w.r.t to γ to see which region is most sensitive (**hot region**).

From the plot on the left, the DCS components are sensitive to γ , as well as the $\rho(770)$

Although the DCS decay is highly suppressed, one have sensitivity on γ due to $\rho(770)$, where the decay fraction $D^0 \rightarrow K_s \rho(770)$ is large. (22% from the fit fraction)

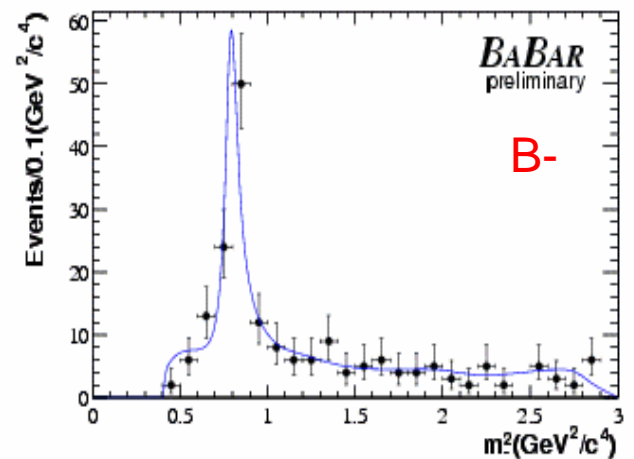
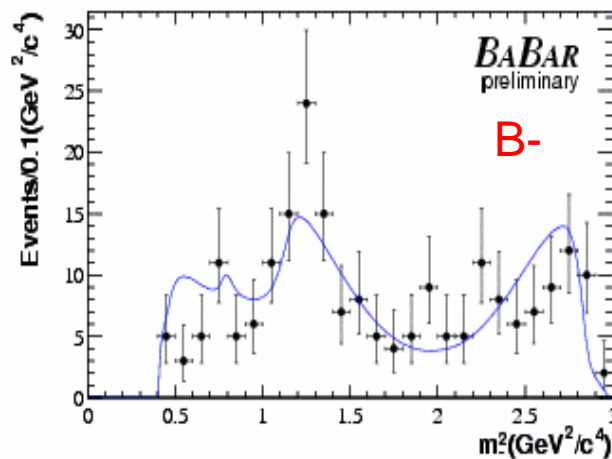
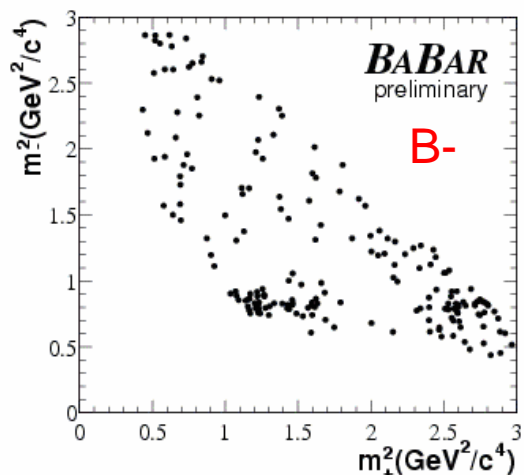
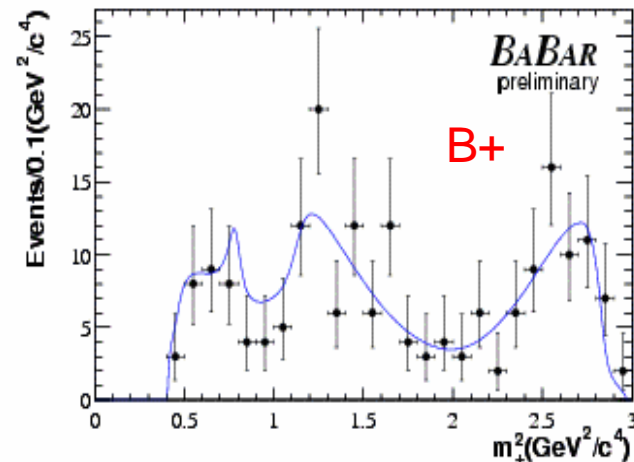
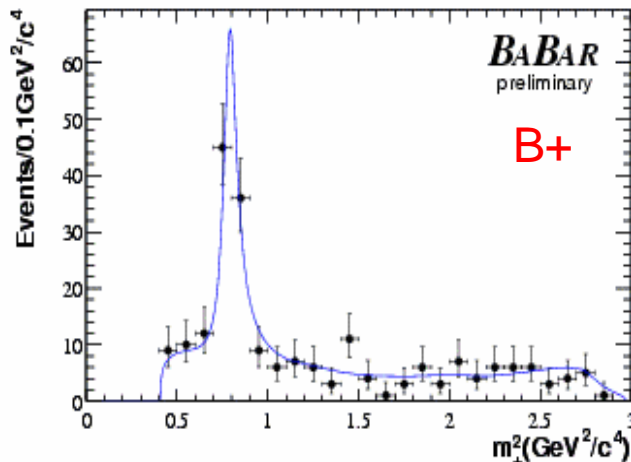
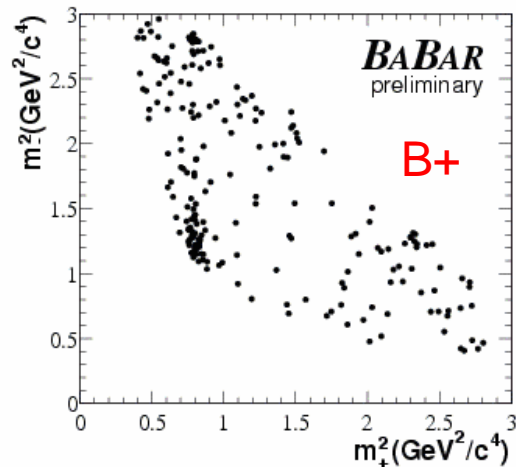
$\rho(770)$

$B^- \rightarrow D^0 K^-$

$$r_b = 0.106^{+0.056}_{-0.054}$$

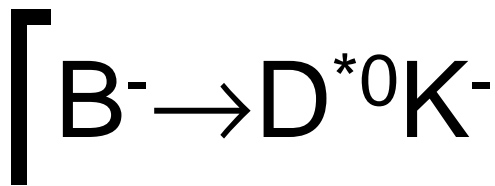
$$d_b = 127^{+30}_{-34}$$

$$g = 66^{+33}_{-30}$$



*Dalitz projection for
 $m_{ES} > 5.272 \text{ GeV}/c^2$*

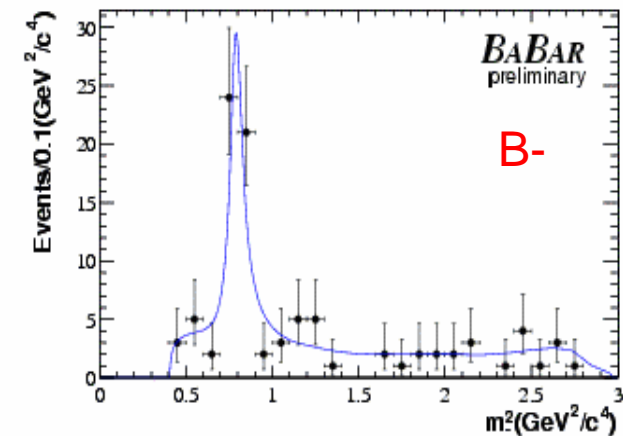
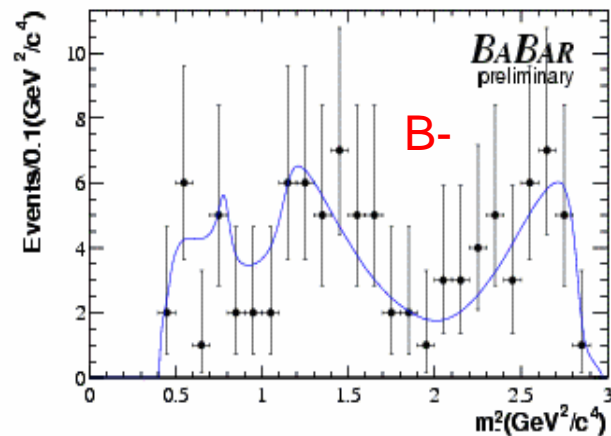
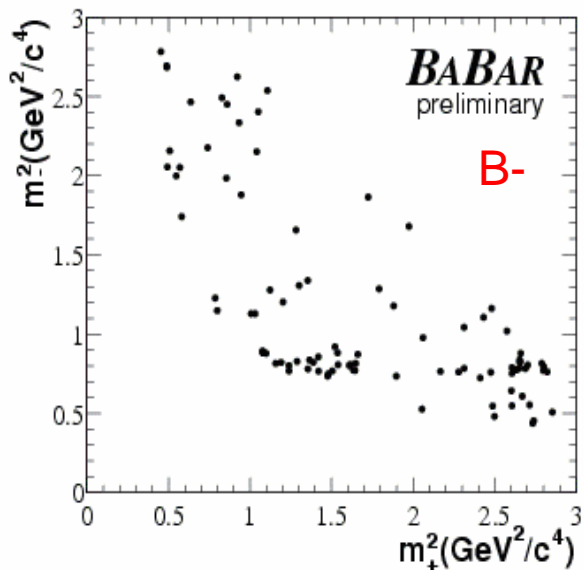
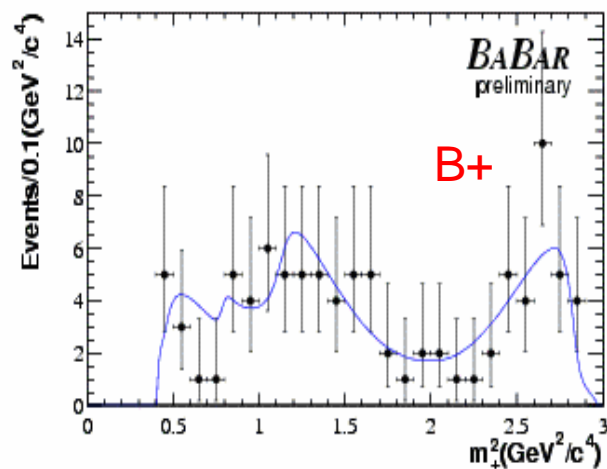
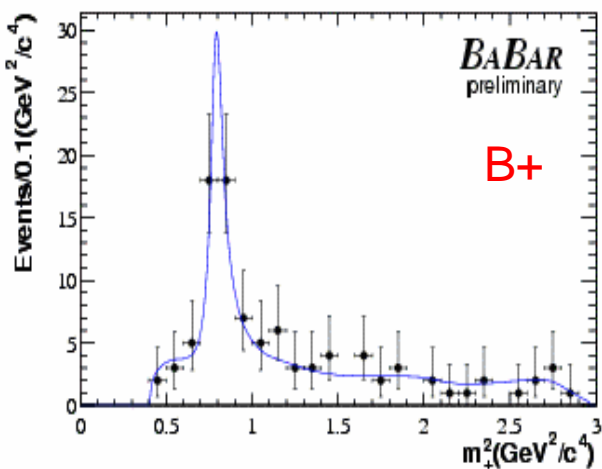
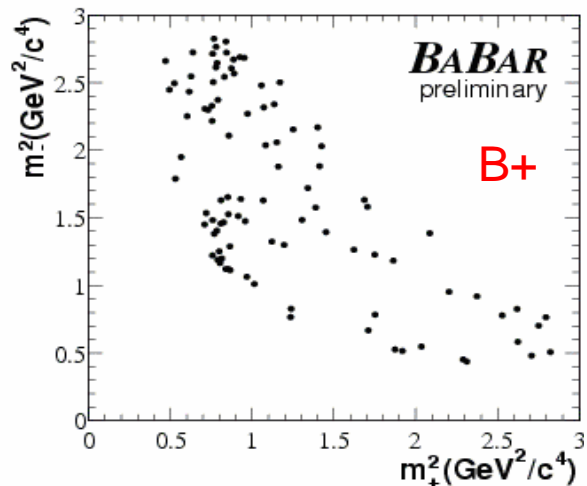
*Signal plus background¹³
PDF superimposed*



$$r_b^* = 0.130^{+0.083}_{-0.076}$$

$$d_b^* = 309^{+33}_{-46}$$

$$g = 120^{+37}_{-39}$$

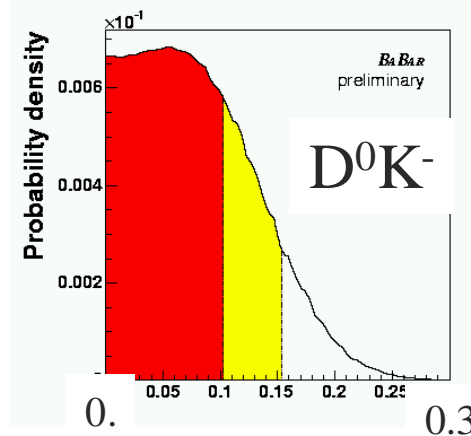
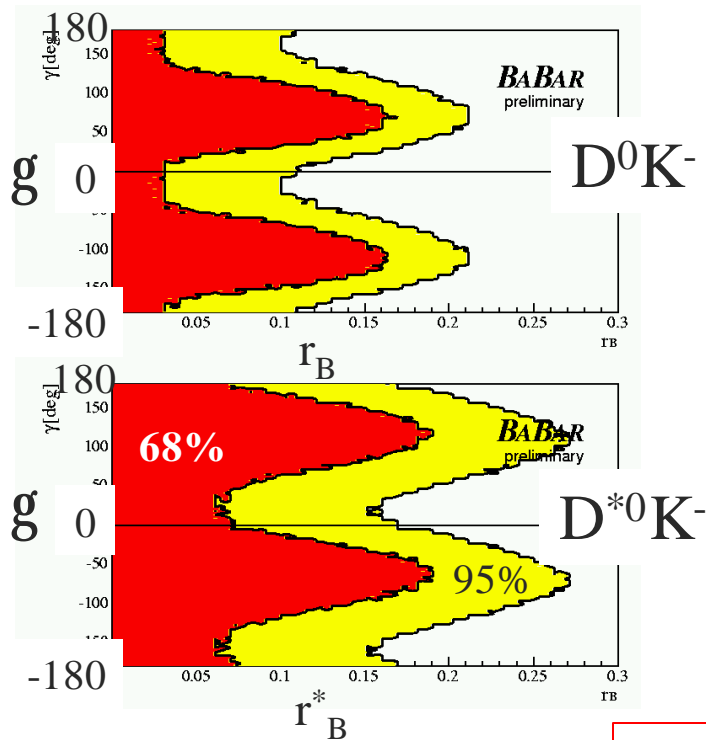
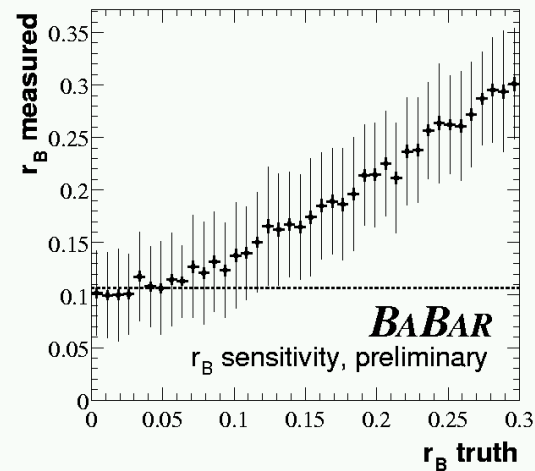


Dalitz projection for $m_{ES} > 5.272 \text{ GeV}/c^2$

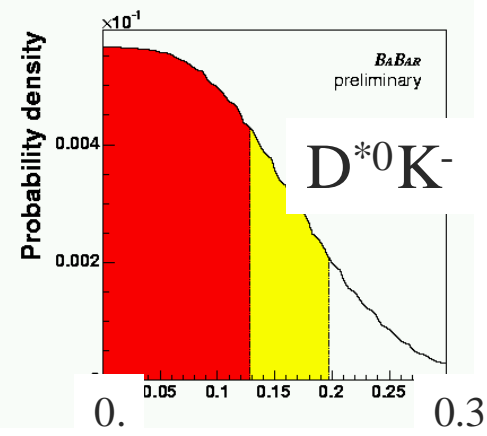
Signal plus background PDF superimposed

γ from $B^- \rightarrow D^{(*)0} [K_S \pi^+ \pi^-] K^-$

With current statistics, no r_B sensitivity for $r_B < 0.10$



$r_b < 0.15$ (95% CL)



$r_b^* < 0.2$ (95% CL)

$$d_B = (130 \pm 45 \pm 8 \pm 10)^{\circ}$$

$$d_B^* = (311 \pm 52 \pm 23 \pm 10)^{\circ}$$

Bayesian
confidence regions

$$g = (88 \pm 41 \pm 19 \pm 10)^{\circ}$$

10° dalitz model systematics

Model systematics error

We tried the following (alternative) models to estimate the model systematics error

Alternative model:

1. Fitting with CLEO 10 resonances model
2. The nominal fit without $\sigma(500)$

} 10^0 model error

Uncertainty in Form Factor:

2. Using Relativistic Breit-Wigner Form Factor instead of more accurate Gounaris-Sakurai parameterization for $\rho(770)$
3. Set Blatt-Weisskopf penetration factor to 1.0

} $\sim 2^0$ model error

Uncertainty in mass and width of establish resonances.

4. Alternative parameterization for $f_0(1370)$ from WA 102 experiment.
5. Shifting $K^*(892)$ mass by +1MeV

} $\sim 2^0$ model error

Uncertainty in amplitude and phase.

6. Vary DCS $K^*(892)$ amplitude and phase

We take 10^0 as the model systematics

Other systematics error

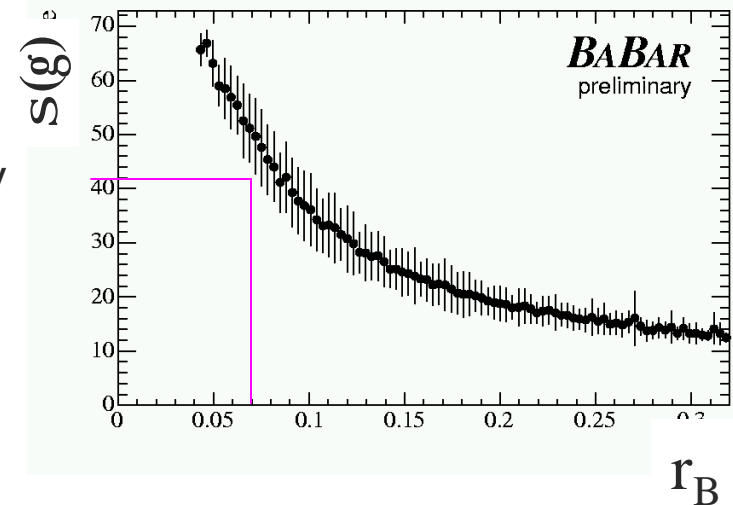
	B- \rightarrow D ⁰ K-	B- \rightarrow D ^{*0} K-
Uncertainty in background dalitz shape:	$\sim 7^{\circ}$	$\sim 3^{\circ}$
Uncertainty in mES, DE, F PDF shape:	$\sim 5^{\circ}$	$\sim 17^{\circ}$
Uncertainty in Efficiency:	$\sim 3^{\circ}$	$\sim 3^{\circ}$
Uncertainty in dalitz amplitude and phase:	$\sim 2^{\circ}$	$\sim 6^{\circ}$
Uncertainty in R(wrong sign tagging rate):	$\sim 2^{\circ}$	$\sim 3^{\circ}$
total	$\sim 10^{\circ}$	$\sim 19^{\circ}$

Conclusion

- B- \rightarrow D⁰K- dalitz plot analysis is one of the promising method to measure CKM γ
- We constraint the $r_b < 0.15$ in the DK mode and $r_b^* < 0.2$ in the D*K mode, while Belle observed large value of r_b
- We measured the CKM γ to be $\gamma = (88 \pm 41 \pm 19 \pm 10)^\circ$ degrees, the large statistical error is due to small r_b value.

- In addition, the dalitz plot analysis on the D* \rightarrow D⁰ π provide a new insight on charm meson spectroscopy

Toy MC study





■ The END!

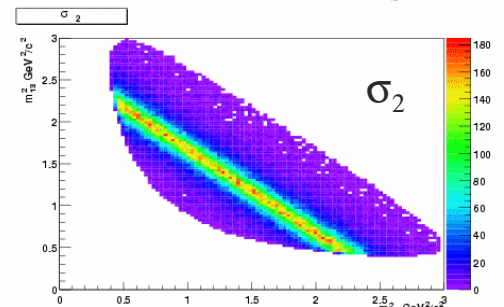
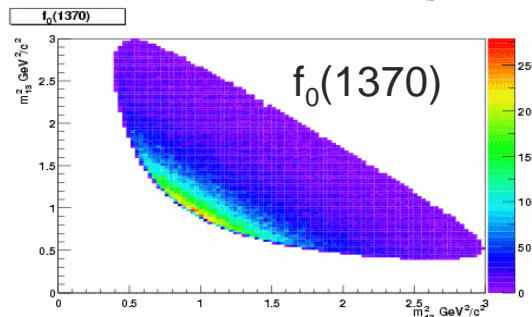
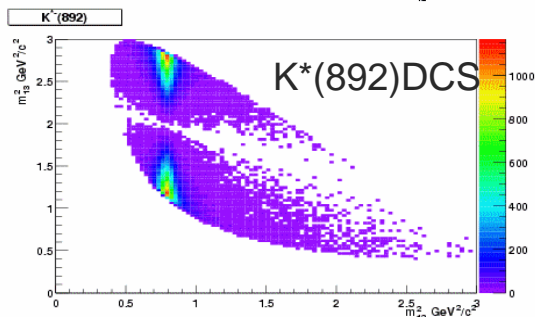
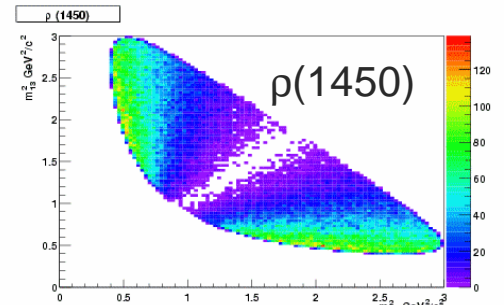
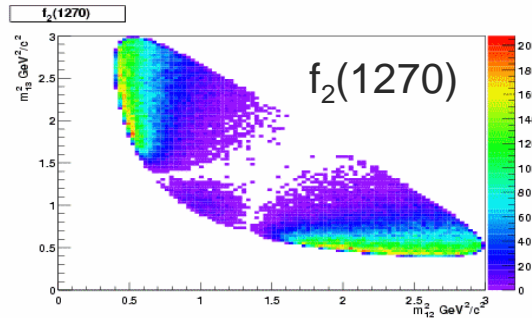
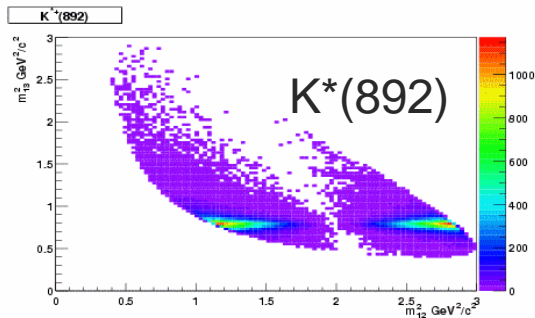
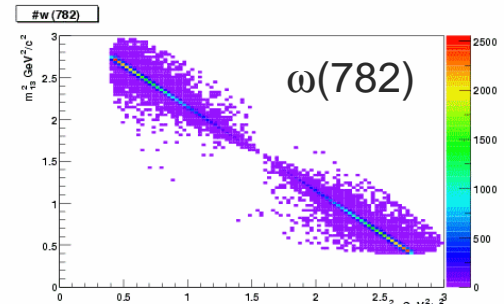
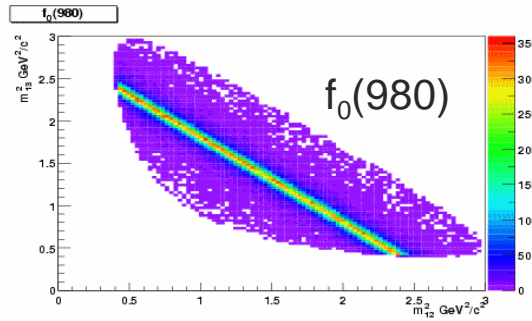
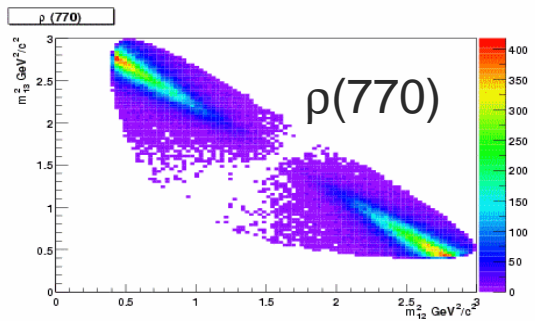


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Backup slides
(the supporting materials)

Dalitz plot at a glance



Dalitz plot at a glance

