

# Determination of $V_{ub}$ from Tagged and Untagged $B\bar{B}$ Events with BABAR



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(supported by the A.v.Humboldt Foundation)



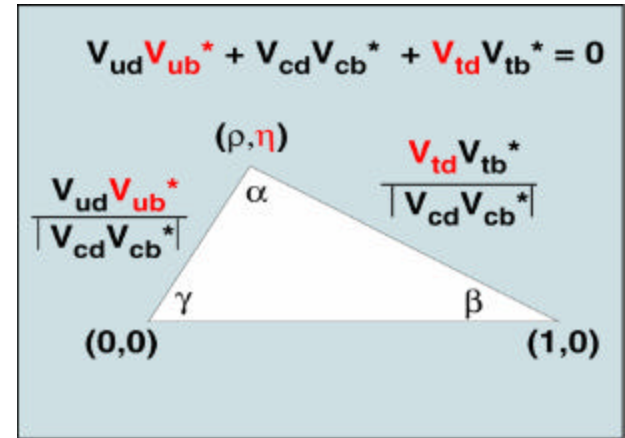
DPF Meeting, Riverside, 26-31 August 2004

# Introduction: $b \rightarrow u \ell \bar{\nu}$ Decays and $V_{ub}$

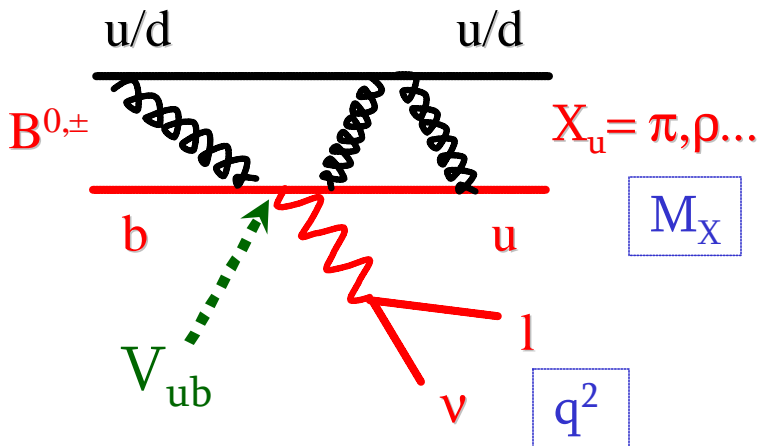
Current progress in determination of CKM matrix element  $|V_{ub}|$  comes from **charmless semileptonic** B decays,  $B \rightarrow X_u \ell \bar{\nu}$ .

## Experimentally challenging:

- **Charm background**  $B \rightarrow X_c \ell \bar{\nu}$  (50 x higher)
- Tight cuts needed and signal analyzed in **limited region of phase space**.
- Large uncertainties from extrapolation.



## Two approaches:

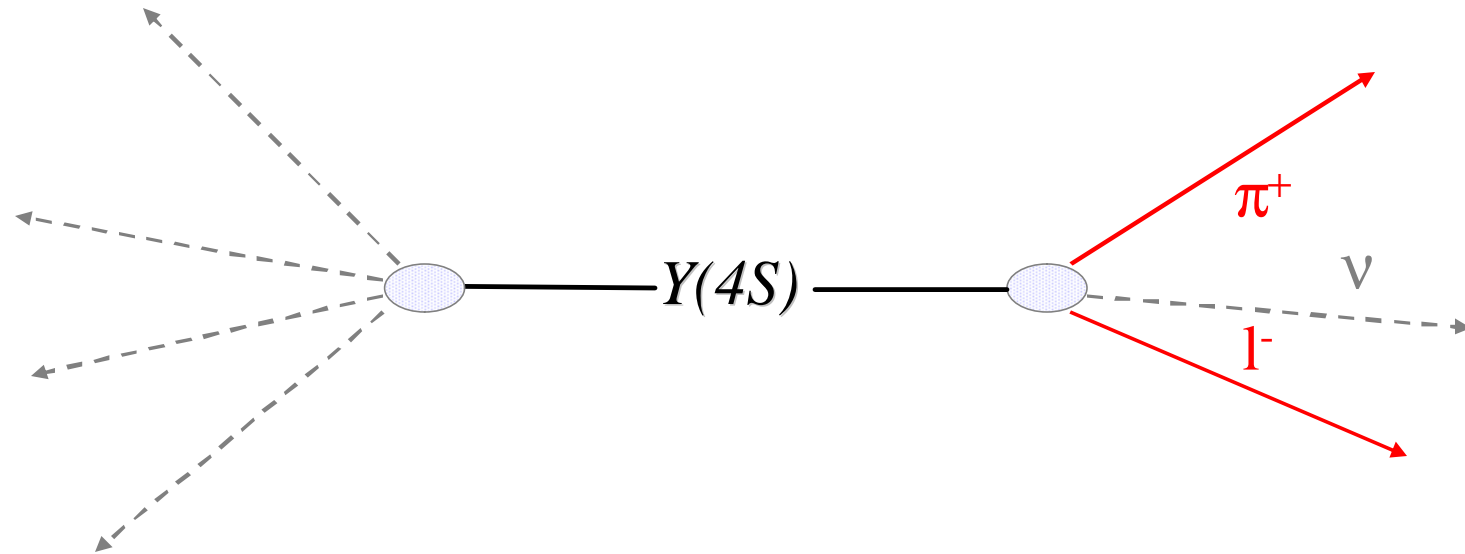


1. **Inclusive:** Look at **kinem. quantities inclusively**.  
Use duality assumption and study  $b \rightarrow u \ell \bar{\nu}$ .  
From total  $B(b \rightarrow u \ell \bar{\nu})$  extraction of  $|V_{ub}|$  with small uncertainties.
2. **Exclusive:** Full **reconstruction of resonances**.  
Need decay form factors to extract branching ratio and  $|V_{ub}|$ .

# Experimental Techniques

Tag Side

Signal Side



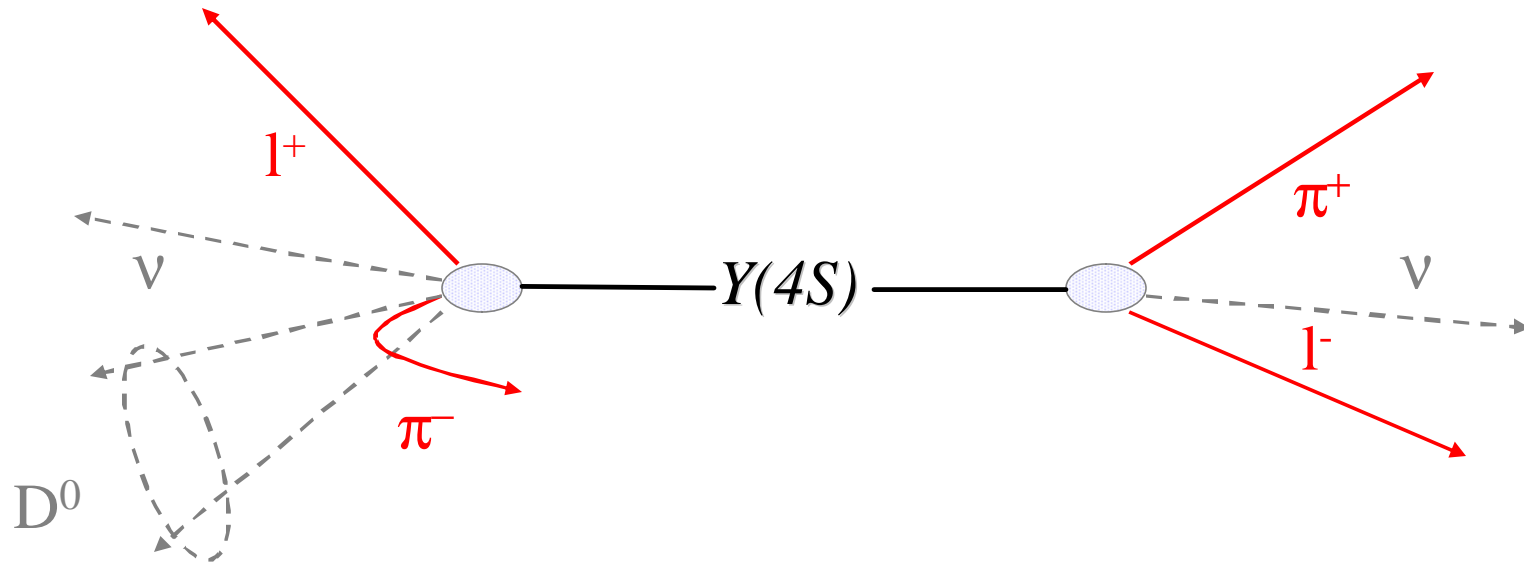
Untagged

No recoil, n reco.  
from miss. momentum

# Experimental Techniques

Tag Side

Signal Side



Untagged

Partial Tags

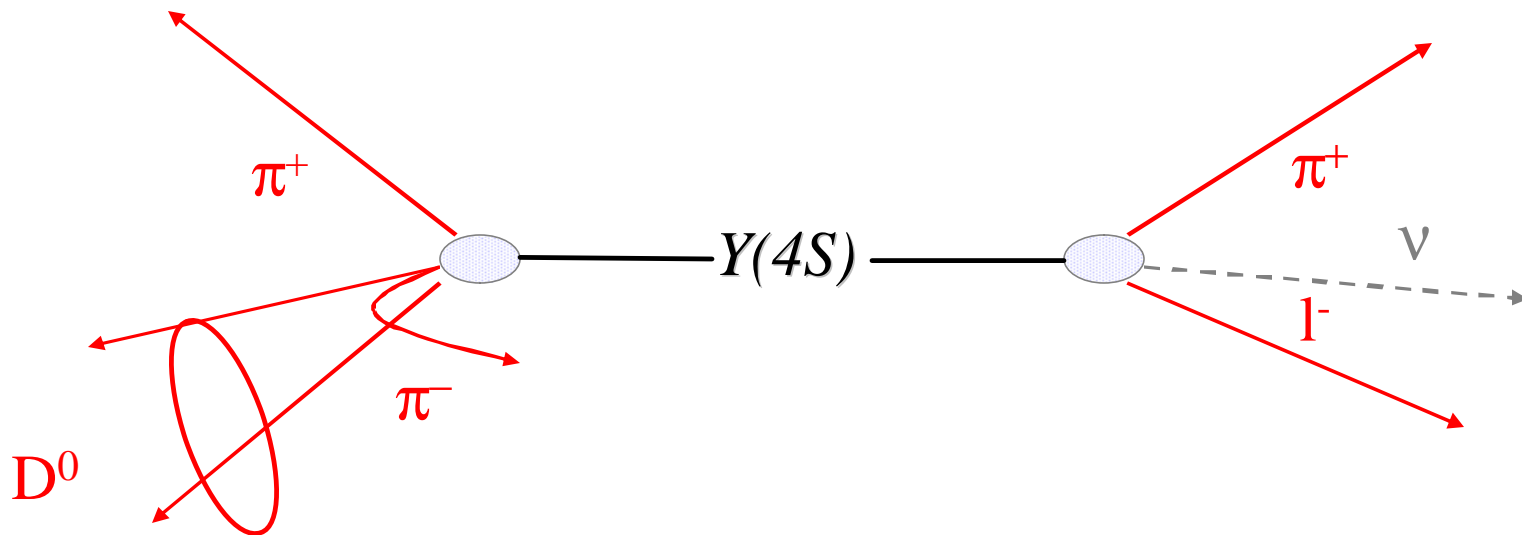
No recoil, n reco.  
from miss. momentum

Recoil of partially  
reco.  $D^*$

# Experimental Techniques

Tag Side

Signal Side



Untagged

No recoil, n reco.  
from miss. momentum

Partial Tags

Recoil of partially  
reco.  $D^*$

Breco Tags

Recoil of fully  
reco.  $B @ D^{(*)} X$

# Inclusive: Lepton Endpoint

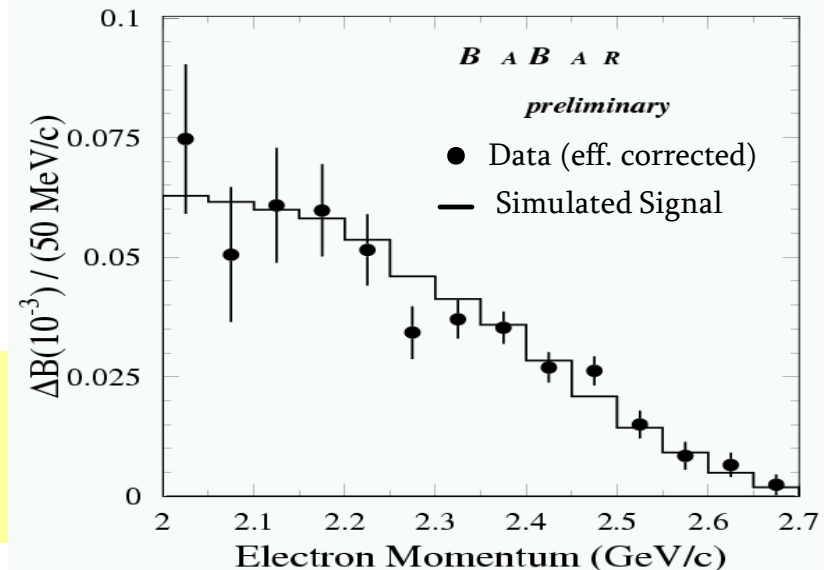
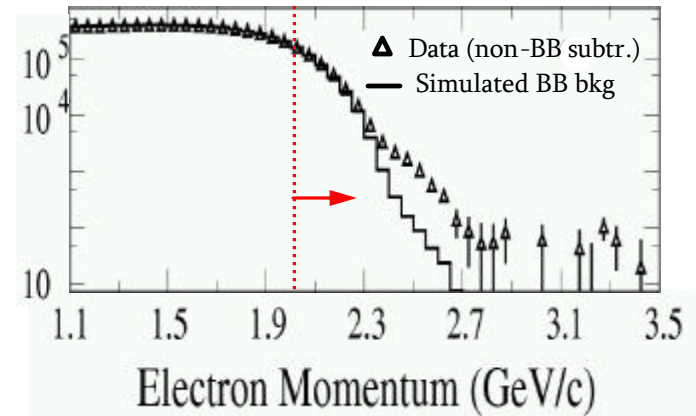
Untagged,  $80 \text{ fb}^{-1}$

## Analysis Strategy:

- One **high energy electron**  
 $2.0 \text{ GeV} < E_e < 2.6 \text{ GeV}$
- Cut on missing momentum  
 $P_n = P_{e^+e^-} - P_{\text{visible}}$
- **Event shape** to suppress continuum:  
 $e^+e^- \text{ @ } l^+l^- / qq$   
**Non-BB bkg** taken from off-peak data  
(on-peak data for  $E_e > 2.8 \text{ GeV}$ ).
- **BB bkg** from fit to  $E_e$  spectrum  
(Den,  $D^*en$ ,  $D^{**}en$ ,  $D^{(*)}pen$ ,  $X_u en$ , non-sl)

$$\text{BR}(B \text{ @ } X_u en) = (1.73 \pm 0.22_{\text{exp}} \pm 0.33_{f_u}) \times 10^{-3}$$

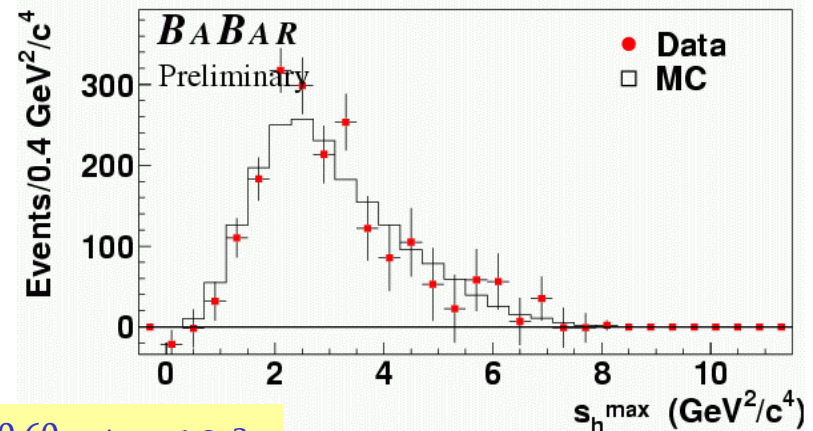
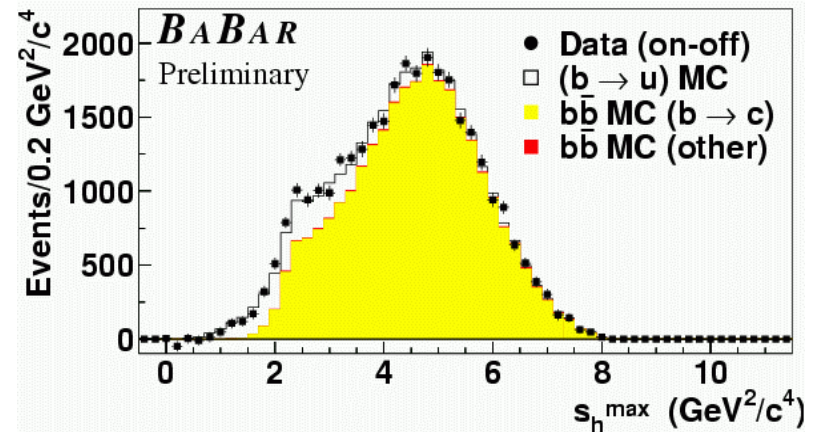
$$|V_{ub}| = (3.94 \pm 0.25_{\text{exp}} \pm 0.37_{f_u} \pm 0.19_{\text{theo}}) \times 10^{-3}$$



# Inclusive: n Reconstruction

Untagged, 80 fb<sup>-1</sup>

- Similar approach as endpoint method ( $p_e^* > 2 \text{ GeV}/c$ ) and **n reco.** from missing momentum and energy. Improved S/B in restricted region of  $q^2$ - $E_e$  plane ( $q^2 = (p_e + p_n)^2$ ).
- **b<sup>0</sup>cln** background separated using max. kinem. allowed hadronic mass squared:
 
$$s_h^{\text{max}}(E_e, q^2) < 3.5 \text{ GeV}^2/c^4 \sim m_D^2$$
 Less sensitive to SF parameters than  $M_X$ .
- Use **B<sup>0</sup>D<sup>0</sup>ln(X)** control sample to check efficiency and shape modeling



$$\text{BR}(B^0 \rightarrow X_u \text{en}) = (2.37 \pm 0.22_{\text{stat}} \pm 0.26_{\text{exp}} \pm 0.34_{\text{bkg}}^{+0.60}_{-0.30 \text{ SF}}) \times 10^{-3}$$

$$|V_{ub}| = (4.57 \pm 0.21_{\text{stat}} \pm 0.25_{\text{exp}} \pm 0.34_{\text{bkg}}^{+0.59}_{-0.29 \text{ SF}} \pm 0.22_{\text{HQE}}) \times 10^{-3}$$

# Incl. Decays: Theoretical Issues

## Sources of theo. uncertainties:

- **Hadronization effects**
- **b quark mass** and **Fermi motion** inside B meson, described by non-perturbative **Shape Function (SF)**.

## Two approaches to extract $|V_{ub}|$ :

### 1. DeFazio-Neubert (DFN):

Extrapolation to total BR using  $d^3G/dq^2dE_1dM_X$ .

$$|V_{ub}| = 0.00424 \sqrt{\frac{B(B \rightarrow X_u \ln)}{0.002} \frac{1.61 ps}{t_B}} \times (1 \pm 0.028_{OPE} \pm 0.039_{m_b})$$

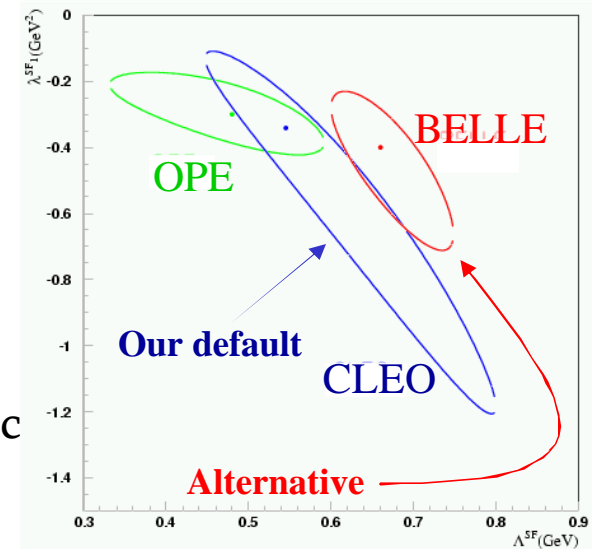
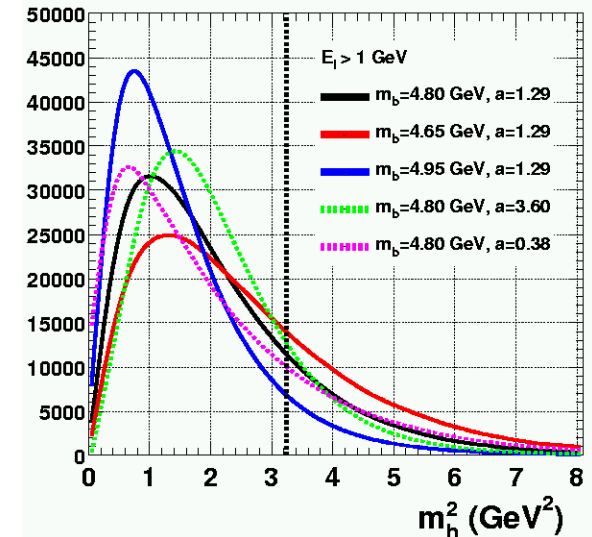
### 2. Bauer-Ligeti-Luke (BLL):

Relates partial BR in restricted  $q^2 - M_X$  region to  $|V_{ub}|$ .

$$|V_{ub}| = \sqrt{\frac{192 p^3}{t_B G_F^2 m_b^5} \frac{\Delta B(B \rightarrow X_u \ln; m_x < 1.7 GeV/c^2, q^2 > 8 GeV^2/c^4)}{G}}$$

Reduced dependence on SF in this region of phase space

Estimate uncertainties from non-perturbative effects using  $I^{SF}$  and  $L^{SF}$  ellipse from CLEO b<sup>®</sup>sg (also recent result from BELLE available).



# Inclusive: $M_X$ and $q^2$

Extension of measurement published in PRL92, 071802.

Breco Tags

## Recoil selection and reconstruction of hadronic system X:

Exactly one lepton with  $p^* > 1 \text{ GeV}/c$

Correlation lepton charge -  $B_{\text{reco}}$  flavor

Missing mass  $M_{\text{miss}}^2 < 0.5 \text{ GeV}^2$ ,

$B^0 @ D^* 1 n$  suppression: partial n reconstruction

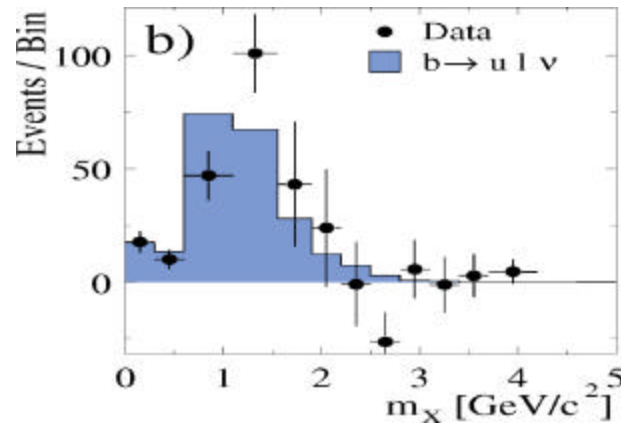
Kaon veto

Kinematic fit (2-C) to improve  $M_X$  resolution

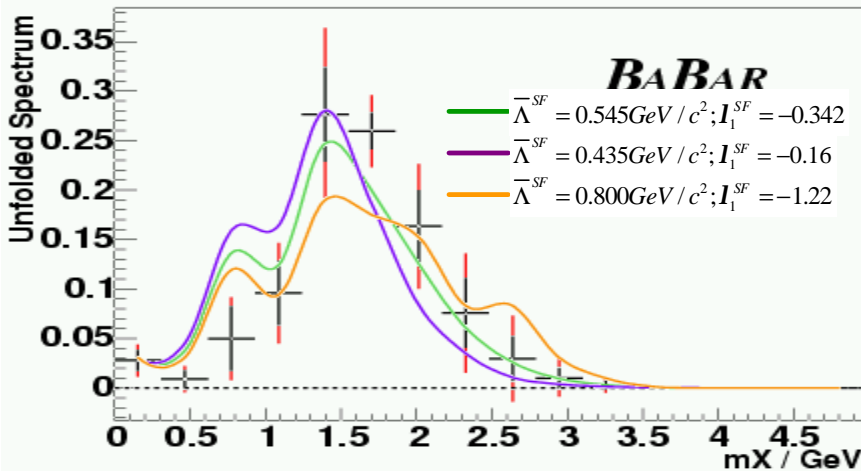
- Measure **ratio of branching fractions**:  $R_{u/sl} = \frac{B(B \rightarrow X_u ln)}{B(B \rightarrow X ln)}$ 
  - ➔ reduced systematics (from lepton ID , tag normalization)
- **Unfold the  $M_X$  spectrum** using same approach and selection
- Approach suggested by Bauer et al.: **Cut on  $M_X$  and  $q^2$** 
  - ➔ reduced dependence on shape function parameters

# Inclusive: $M_X$

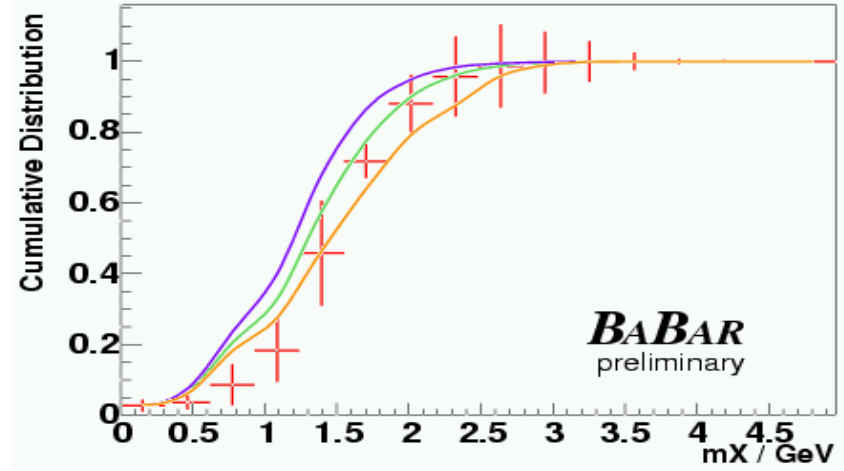
Breco Tags,  $80 \text{ fb}^{-1}$



Unfolded  $M_X$  spectrum



Cumulative  $M_X$  distribution

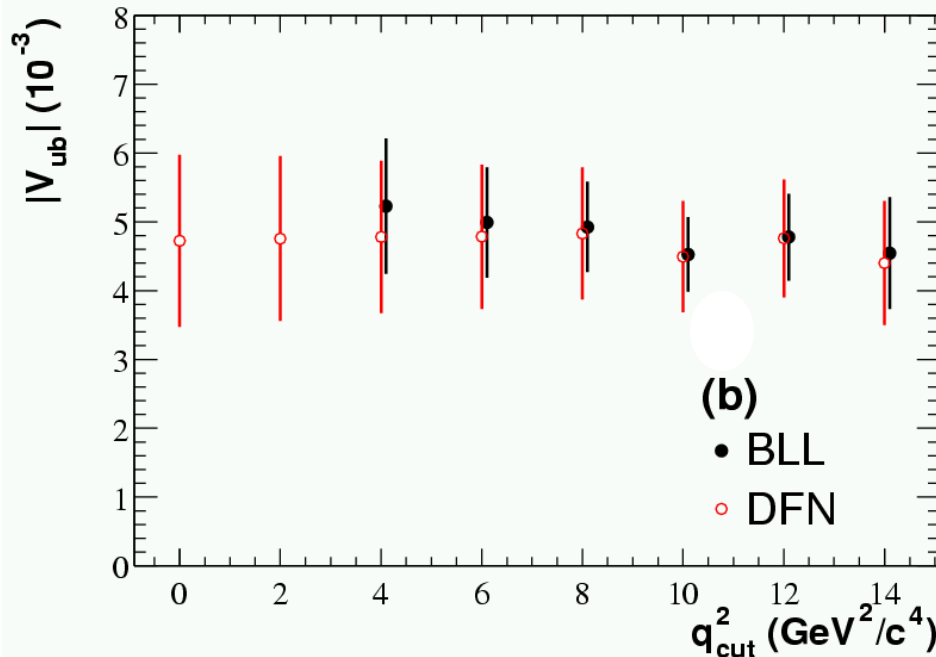


- Unfolding of detector and selection effects:  $\vec{x}_{\text{meas}} = A_{\text{detector-resp.}} \vec{x}_{\text{true}}$
- With higher statistics,  $M_X$  moments can be used to constrain SF parameters.

# Inclusive: $M_X$ vs. $q^2$

Breco Tags,  $80 \text{ fb}^{-1}$

$|V_{ub}|$  as a function of  $q^2$  cut



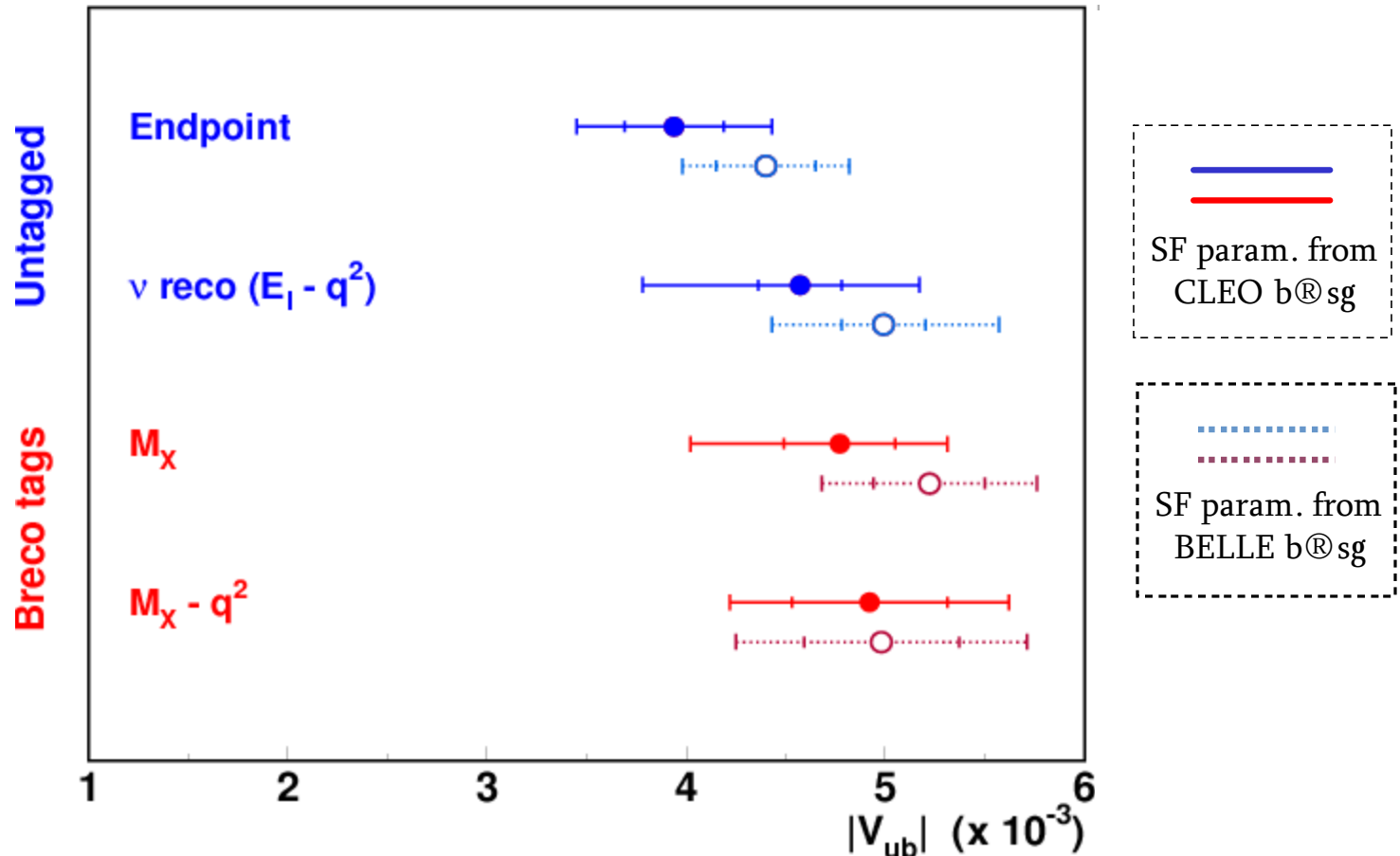
- DBR from phase space region where SF effects are small:  
 $M_X < 1.7 \text{ GeV}$  and  $q^2 > 8 \text{ GeV}^2$
- $|V_{ub}|$  stable wrt variation of cut on  $q^2$
- Good consistency between theoretical frameworks

$$\text{DBR}(B \rightarrow X_u \text{en}) = (0.88 \pm 0.14_{\text{stat}} \pm 0.13_{\text{exp}} \pm 0.13_{\text{theo}}) \times 10^{-3}$$

$$|V_{ub}| = (4.92 \pm 0.39_{\text{stat}} \pm 0.36_{\text{exp}} \pm 0.46_{\text{theo}}) \times 10^{-3}$$

# BABAR Inclusive Measurements Overview

Comparison of  $|V_{ub}|$  measurements using different techniques



- Dominant systematic uncertainty from modeling of non-perturbative effects.
- Results compared for SF parameters from CLEO (2001) and BELLE (2004).

# Exclusive Decays on the Recoil

## Partial Tags

s.l. tags  $B^0 @ D^* l n$

Fits to **missing mass**  $M_n^2$  spectrum to extract signal yields.  
Measurement in **three bins of  $q^2$**  (0 – 8 – 16  $\text{GeV}^2/c^4$ ).

$$\text{BR}(B^0 @ p^- l^+ n) = (1.46 \pm 0.27_{\text{stat}} \pm 0.35_{\text{syst}}) \times 10^{-4}$$

## Breco Tags

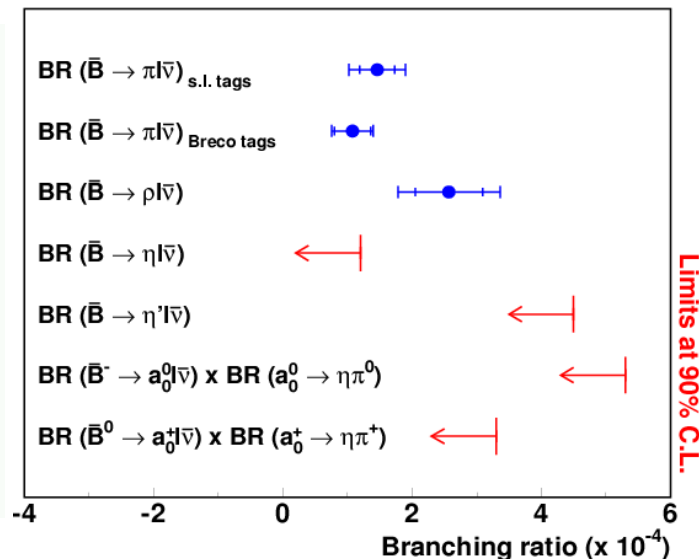
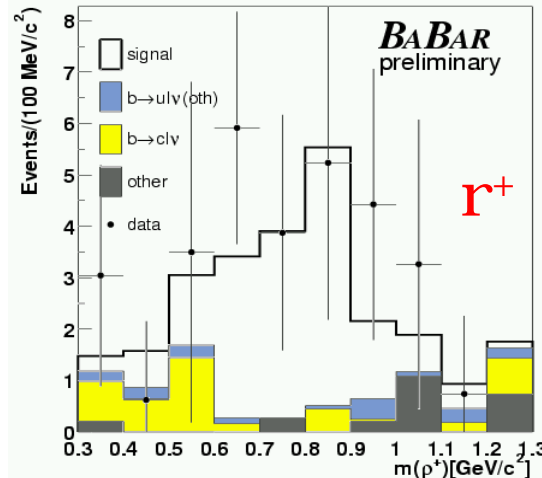
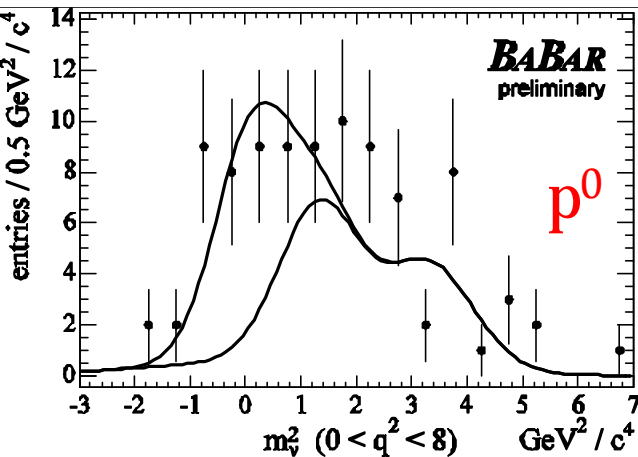
$B @ X_u l n$  modes:  $X_u = p^+, p^0, r^+, r^0, w, h, h', a_0^0, a_0^+$

Similar to inclusive Breco analysis, but with **exclusively fully reconstructed resonances**.

$$\text{BR}(B^0 @ p^- l^+ n) = (1.08 \pm 0.28_{\text{stat}} \pm 0.16_{\text{syst}}) \times 10^{-4}$$

$$\text{BR}(B^0 @ r^- l^+ n) = (2.57 \pm 0.52_{\text{stat}} \pm 0.59_{\text{syst}}) \times 10^{-4}$$

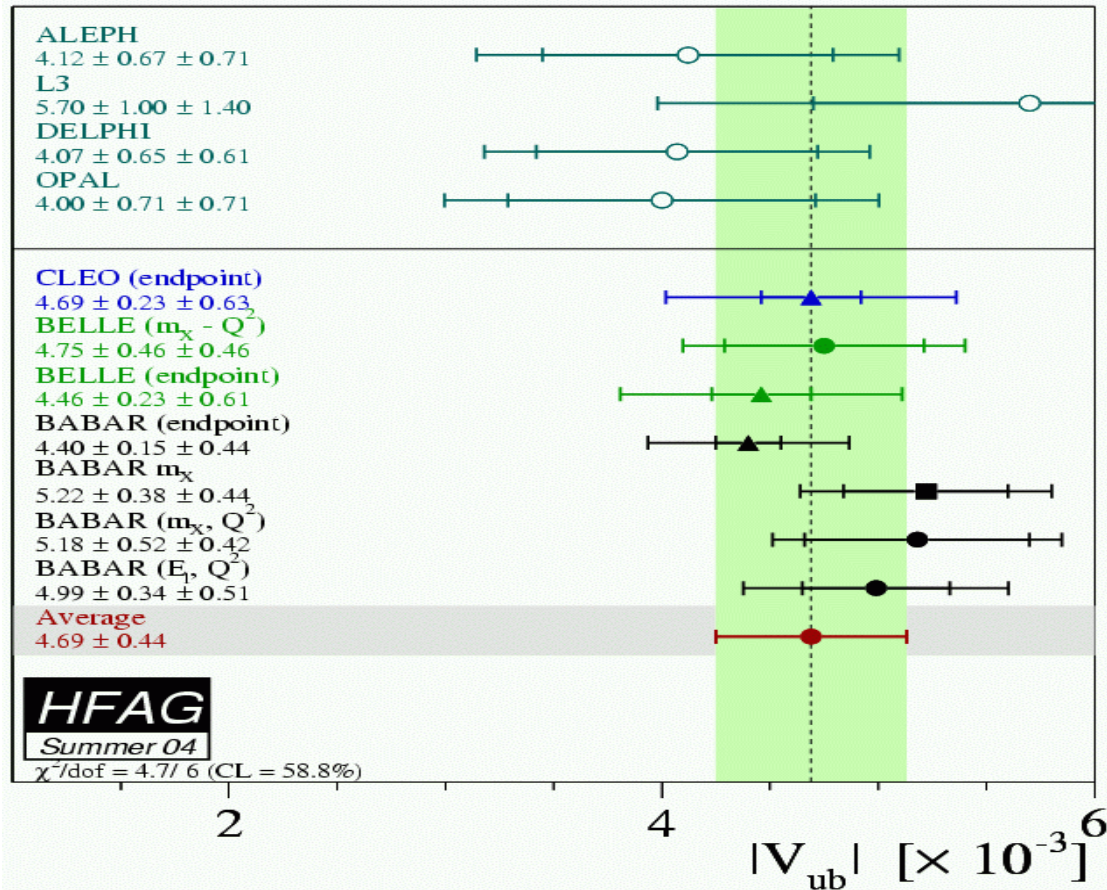
Set upper limits  
for  $h, h', a_0^0, a_0^+$



# Summary: $V_{ub}$ at BABAR

	Analysis Method	S/B	Pros & Cons	$V_{ub} (\times 10^{-3})$
Electron endpoint	Inclusive, untagged $E_e > 2.0 \text{ GeV}$ Total rate using DFN	0.05 .. 0.2	<ul style="list-style-type: none"> <li>• High statistics</li> <li>• Duality valid for harsh <math>E_e</math> cuts?</li> <li>• Bkg subtraction</li> </ul>	$3.94 \pm 0.25_{\text{exp}} \pm 0.42_{\text{theo}}$
n reconstruction ( $E_e$ vs. $q^2$ )	Inclusive, untagged $E_e > 2.0 \text{ GeV}$ and $s_h < 3.5 \text{ GeV}^2/c^4$ Total rate using DFN	0.5	<ul style="list-style-type: none"> <li>• High statistics</li> <li>• Lower syst. on shape functions</li> <li>• Bkg subtraction</li> </ul>	$4.57 \pm 0.47_{\text{exp}} \begin{matrix} +0.62 \\ -0.36 \text{ theo} \end{matrix}$
$M_X$ analysis	Inclusive, Breco tag $m_X < 1.55 \text{ GeV}/c^2$ Total rate using DFN	1.7	<ul style="list-style-type: none"> <li>• Low background</li> <li>• High resolution</li> <li>• Low statistics</li> <li>• Shape func. syst.</li> </ul>	$4.77 \pm 0.40_{\text{exp}} \begin{matrix} +0.69 \\ -0.45 \text{ theo} \end{matrix}$
$M_X$ vs. $q^2$ analysis	Inclusive, Breco tag $m_X < 1.7 \text{ GeV}/c^2$ , $q^2 > 8.0 \text{ GeV}^2/c^4$ $V_{ub}$ using BLL	2	<ul style="list-style-type: none"> <li>• Low background</li> <li>• Very small syst. on SF param.</li> <li>• Small statistics</li> </ul>	$4.92 \pm 0.53_{\text{exp}} \pm 0.46_{\text{theo}}$
Exclusive analyses on recoil	Exclusive, Partial or Breco tags Total rate using Form Factor calculations	1 .. 20	<ul style="list-style-type: none"> <li>• Very small bkg</li> <li>• Almost no cut on kinematics</li> <li>• Small statistics</li> </ul>	Future (larger statistics)

# Current Status of $V_{ub}$



- In the near future, syst. errors will decrease due to **new measurements of inclusive photon spectrum** and **advances in theo. understanding of the SF**.
- With **higher statistics**, the novel “**clean**” recoil methods will be very fruitful.