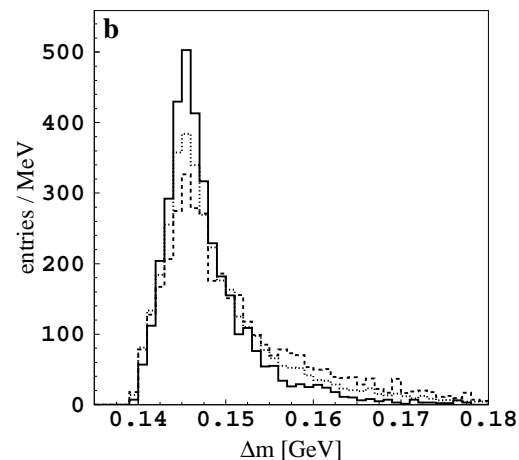
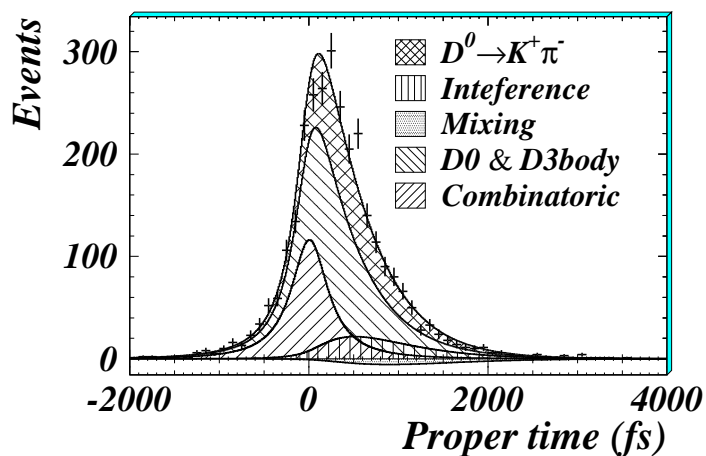


# $D^0-\bar{D}^0$ mixing at Belle

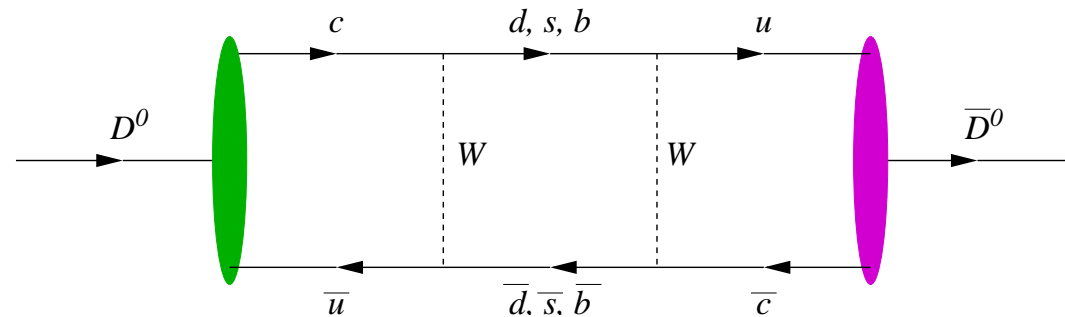


$D^0 \rightarrow K^+\pi^-$ :  $90 \text{ fb}^{-1}$   
 hep-ex/0408125 final

$D^0 \rightarrow K^+e^-\bar{\nu}_e$ :  $140 \text{ fb}^{-1}$   
 hep-ex/0408112 prelim.

Bruce Yabsley (Virginia Tech)

DPF 2004 / UC Riverside, 30th August 2004



- GIM suppression  $\left( (m_s^2 - m_d^2)/m_c^2 \right)^2 \rightarrow$  SM box diagram *tiny*
- higher order diagrams also suppressed (at least  $\sin^2 \theta_C$ )
- OPE estimates:  $\left\{ \begin{array}{l} x = \Delta M/\Gamma \\ y = \Delta\Gamma/2\Gamma \end{array} \right\} \lesssim 10^{-3} \rightarrow R_{mix} \lesssim 10^{-6}$
- $K\pi$ , resonances may raise  $x, y \rightarrow O(10^{-2})$  ???
- New Physics generally adds new box diagrams  
 $\Rightarrow$  enhanced  $x$ ,  $\approx$  unchanged  $y$
- mixing-with-CPV would be a NP smoking gun

$$\frac{dN}{dt} \propto e^{-\bar{\Gamma}t} \left[ R_D + \sqrt{R_D} y'(\bar{\Gamma}t) + \frac{x'^2 + y'^2}{4} (\bar{\Gamma}t)^2 \right]$$

- $\tan^2 \theta_C \gg R_{\text{mix}}^{\text{expected}}$ :  $R_D$  dominates

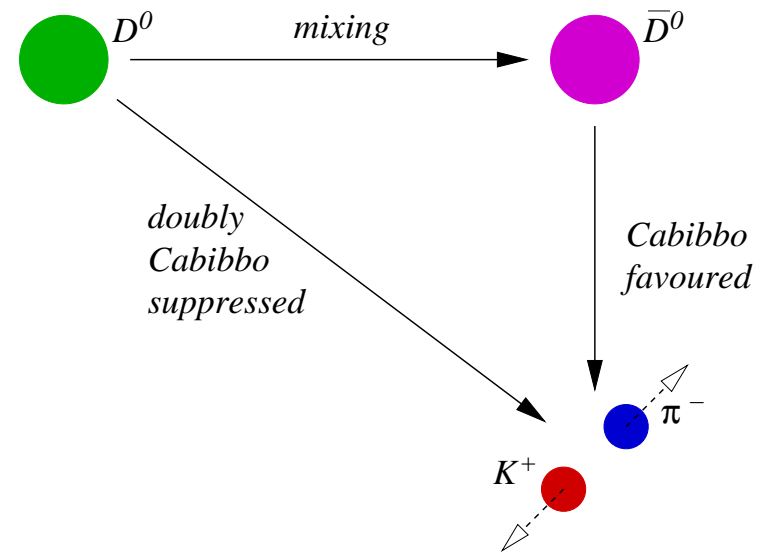
- time dependence disentangles

$e^{-t}$  DCSD

$t \cdot e^{-t}$  interference term

$t^2 \cdot e^{-t}$  mixing

- strong phase difference  $\delta_{K\pi} \rightarrow$   
we measure  $x$  and  $y$  rotated by  $\delta_{K\pi}$



interference term  $f(t) \rightarrow$  sensitivity to mixing

- **categorize** backgrounds by  $f(t)$
- **fix** in the timing fit  $\rightarrow$  recover interference



# $D^0 \rightarrow K^+ \pi^-$ analysis outline



- decay chain  $D^{*+} \rightarrow D^0 \pi^+$ ,  $D^0 \rightarrow K^+ \pi^-$  (“wrong-sign”)
- selection cuts
  - *tracks*: good quality, SVD hits, K/ $\pi$  ID cuts
  - $D^{*+}$ :  $p(D^{*+}) > 2.5 \text{ GeV}/c$  in CM (vs  $B\bar{B}$ , combinatorics)
- vertexing to get  $\left\{ \begin{array}{ll} D^0 \text{ decay point} & \text{from } K^+, \pi^- \\ D^0 \text{ origin} & \text{from extrapolation to IP} \\ \text{better } D^{*+} \text{ quality} & \text{from } \pi^+ \text{ refit to D origin} \end{array} \right.$
- vertexing quality cuts
- $(M, Q)$  fit to determine backgrounds ( $S/B \sim 1$  after cuts)
- *decay-time fit* to  $(M, Q)$  signal box  $\longrightarrow (R_D, y', x'^2)$ 
  - background levels: set from the larger  $(M, Q)$  fit
  - background “decay-time”  $\text{dist}^n$ :  $f_i(t') \otimes \mathcal{R}_{i, \text{data}}(t - t')$
  - signal decay-time  $\text{dist}^n$ :  $f(t'; R_D, y', x'^2) \otimes \mathcal{R}_{\text{data}}(t - t')$



# $D^0 \rightarrow K^+ \pi^-$ : backgrounds [with differing $f(t)$ ]



MC wrong-sign backgrounds ( $\exists$  similar breakdown for right-sign)

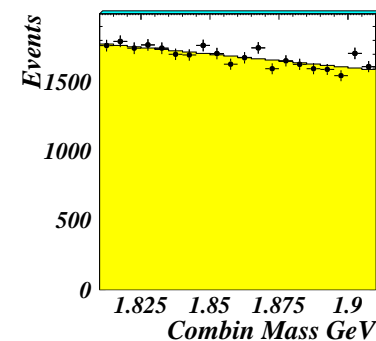
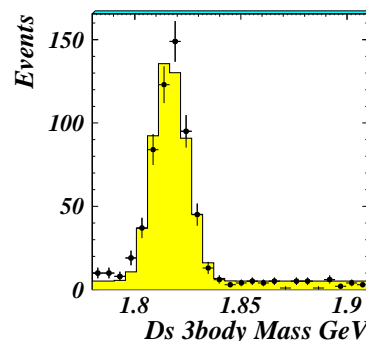
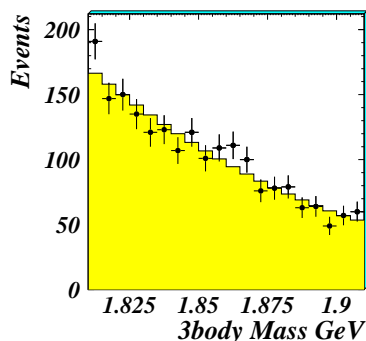
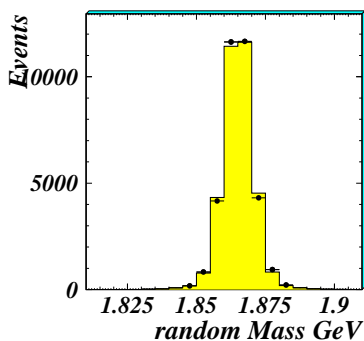
“random  $\pi_{\text{slow}}$ ”

$D^0$  3-body

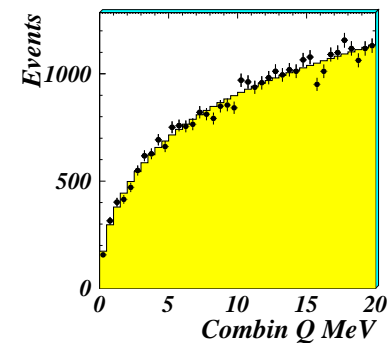
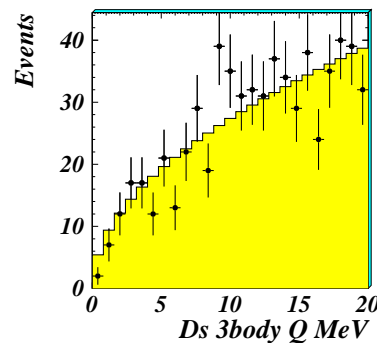
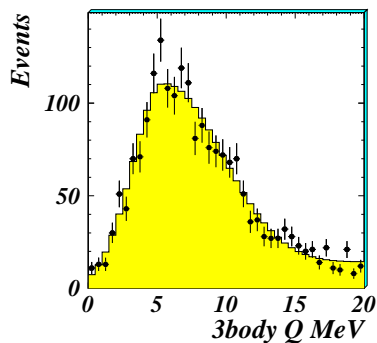
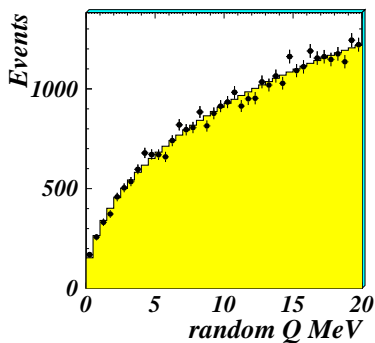
$D^+, D_s^+$

combinatorial

$M$



$Q$



relative normalization of  $D^+, D_s^+ / D^0$  3-body fixed in fit ...

RIGHT-SIGN:

$$N_{RS} = 227\,721 \pm 497$$

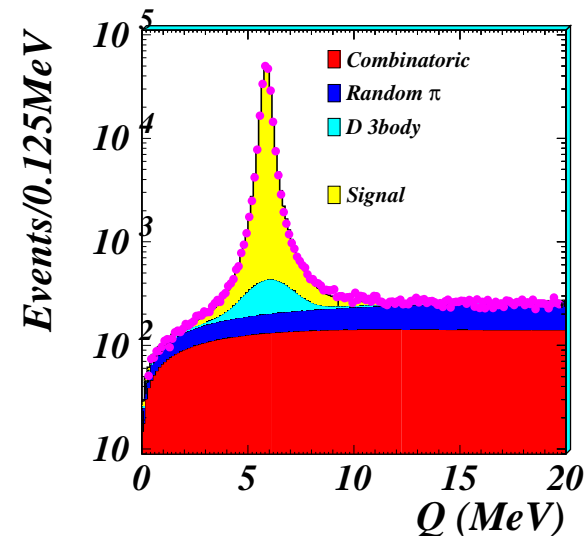
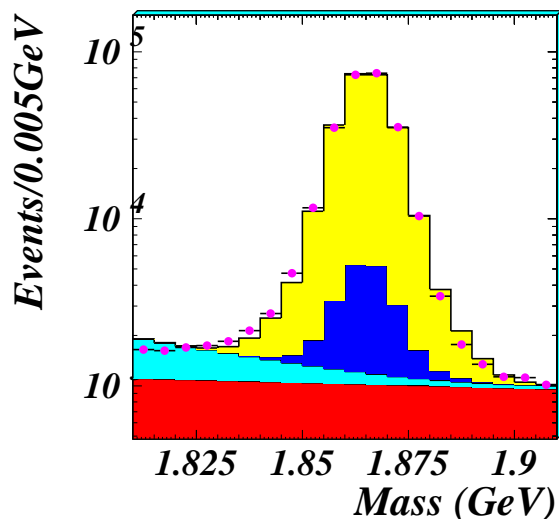
wrong-sign rate

$$R_{WS} \equiv \frac{\Gamma(D^0 \rightarrow K^+ \pi^-)}{\Gamma(D^0 \rightarrow K^- \pi^+)}$$

$$= (0.371 \pm 0.018)\%$$

statistical only

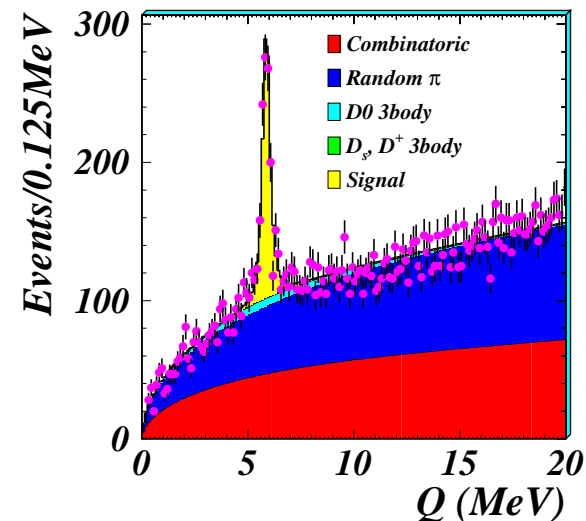
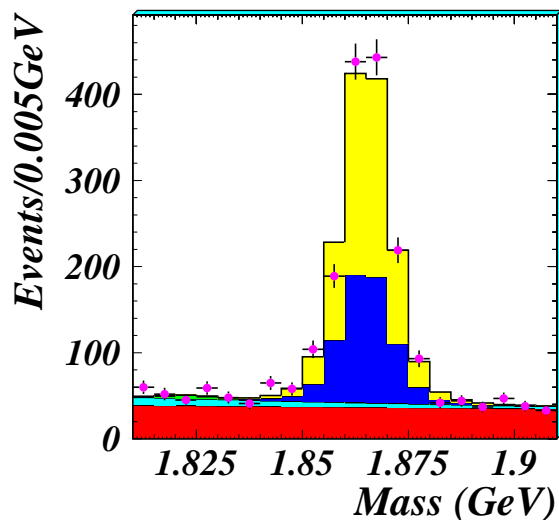
[supersedes earlier  
arXiv:hep-ex/0208051]



WRONG-SIGN:

$$N_{WS} = 845 \pm 40$$

- *Combinatoric*
- *Random  $\pi$*
- *D0 3body*
- *D<sub>s</sub>, D<sup>+</sup> 3body*
- *Signal*





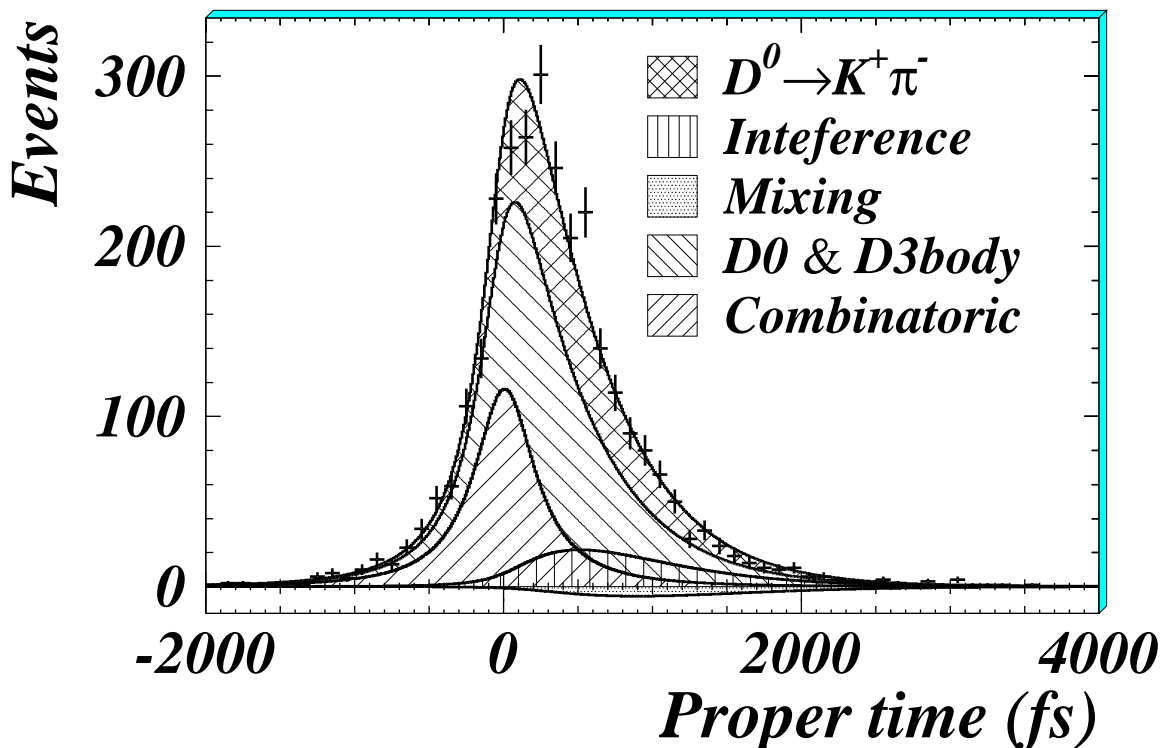
# $D^0 \rightarrow K^+ \pi^-$ : timing fit results ( $/10^{-3}$ )



	$R_D$	$y'$	$x'^2$
mixing fit, $x'$ free:	$2.87 \pm 0.37$	$+25.4^{+11.1}_{-10.2}$	$-1.53^{+0.80}_{-1.00}$
mixing fit, $x'$ fixed:	$3.43 \pm 0.26$	$+6.0 \pm 3.3$	0

project<sup>n</sup> of full  
(M, Q) region:

- $\chi^2/n_{\text{bins}} = 71.9/60$
- $x' = 0$  fixed  $\mapsto$   
 $\chi^2/n_{\text{bins}} = 73.2/60$
- toy MC at  $x' = 0$ :  
 $P(x'^2 < x'^2_{\text{fit}}) = 8\%$
- CPV fits also done  
( $D^0, \bar{D}^0$  separately)  
...





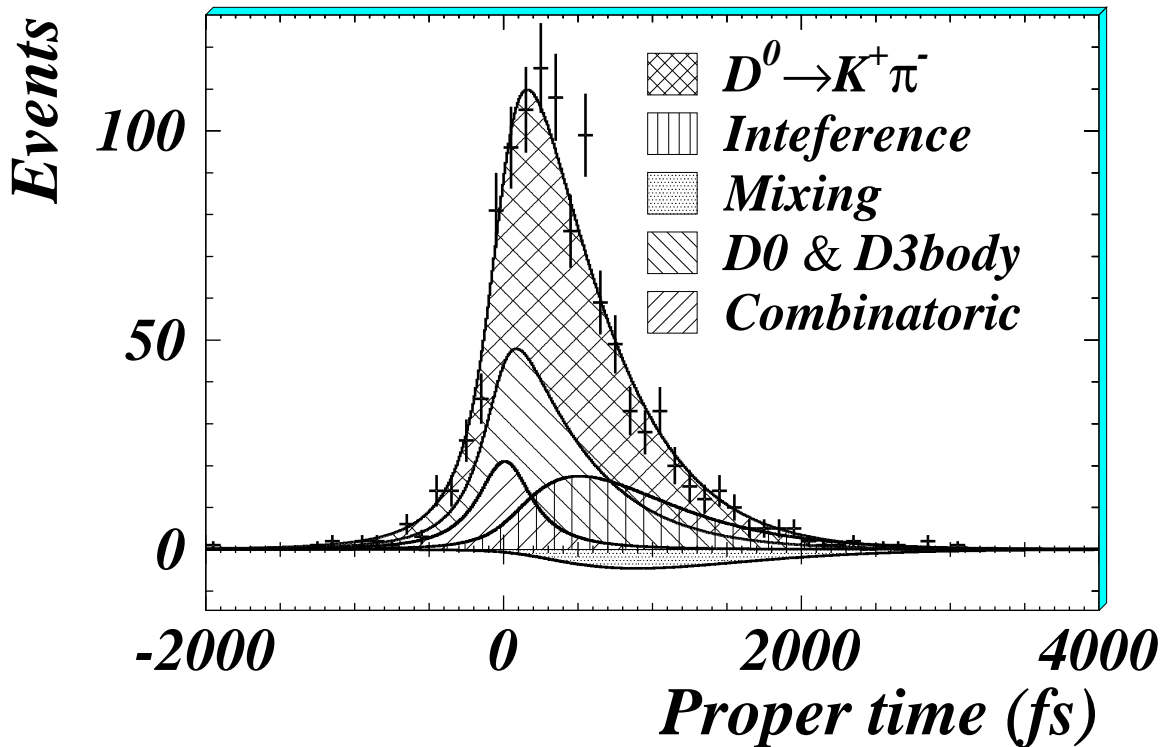
# $D^0 \rightarrow K^+ \pi^-$ : timing fit results ( $/10^{-3}$ )



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mixing fit, $x'$ fixed:	$3.43 \pm 0.26$	$+6.0 \pm 3.3$	0

project<sup>n</sup> of tighter  
( $M, Q$ ) region:

- $\chi^2/n_{\text{bins}} = 71.9/60$
- $x' = 0$  fixed  $\mapsto$   
 $\chi^2/n_{\text{bins}} = 73.2/60$
- toy MC at  $x' = 0$ :  
 $P(x'^2 < x'^2_{\text{fit}}) = 8\%$
- CPV fits also done  
( $D^0, \bar{D}^0$  separately)  
...





A number of checks were performed before unblinding the result:

- consistent time distributions/resolutions/fit procedure
- MC background parameters: sideband  $\sim$  describes signal region
- MC vs. data: resolution functions similar
- right signal region fit:  $\tau_{D^0} = 415.1 \pm 1.4$  ps; good fit
- full MC simulation: fit consistent with input  $(x'^2, y')$
- toy MC simulation: negligible bias  
smeared per full MC

---

95% confidence contours are based on **toy MC** datasets  
generated at (candidate) contour points  $\vec{\alpha} = (x'^2, y')$ :  
the procedure implements **likelihood-ratio ordering**  
*i.e.* Feldman-Cousins



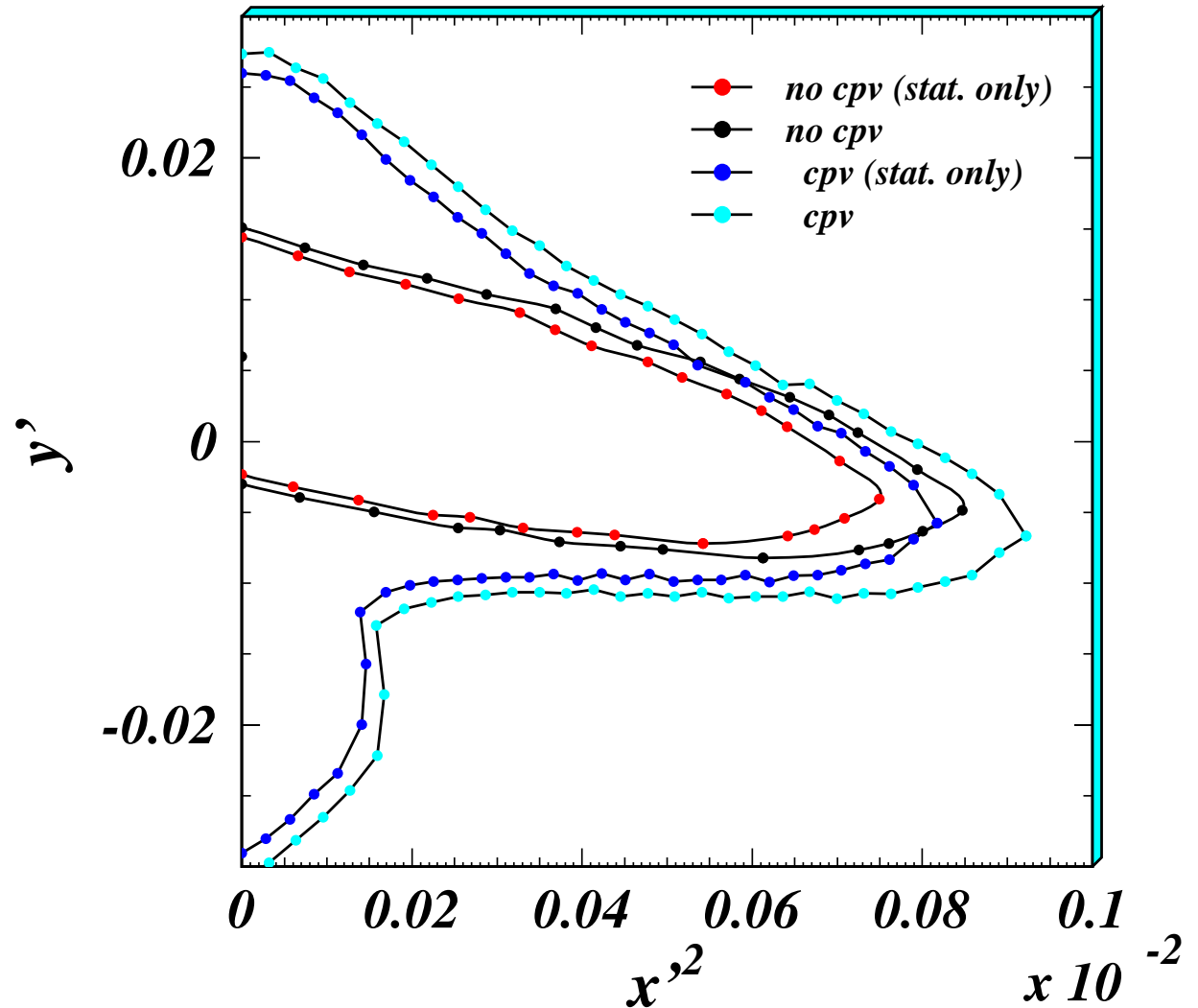
# $D^0 \rightarrow K^+ \pi^-$ : 95% confidence intervals



- improves BaBar  $\sim 2$
- intervals  $\ni (0, 0)$
- systematics: scale contour points by  $\Delta(\text{significance})$

CPV case:

- $D^0$ :  $(R_D^+, x'^{+2}, y'^+)$
- $\bar{D}^0$ :  $(R_D^-, x'^{-2}, y'^-)$
- combine the  $D^0, \bar{D}^0$   
 $1 - \sqrt{0.05} = 77.6\%$   
CL contours
- 2 sol<sup>ns</sup>: take both
- form envelope



$$\frac{dN}{dt} \propto e^{-\bar{\Gamma}t} \left[ \quad + \frac{x'^2 + y'^2}{4} (\bar{\Gamma}t)^2 \right]$$

- no DCS amplitude: decay rate proportional to  $R_{\text{mix}}$
- we can still use the time dependence:

$e^{-t}$  mistagged  $D^0$ -decay background

$t \cdot e^{-t}$  NO INTERFERENCE TERM

$t^2 \cdot e^{-t}$  mixing signal

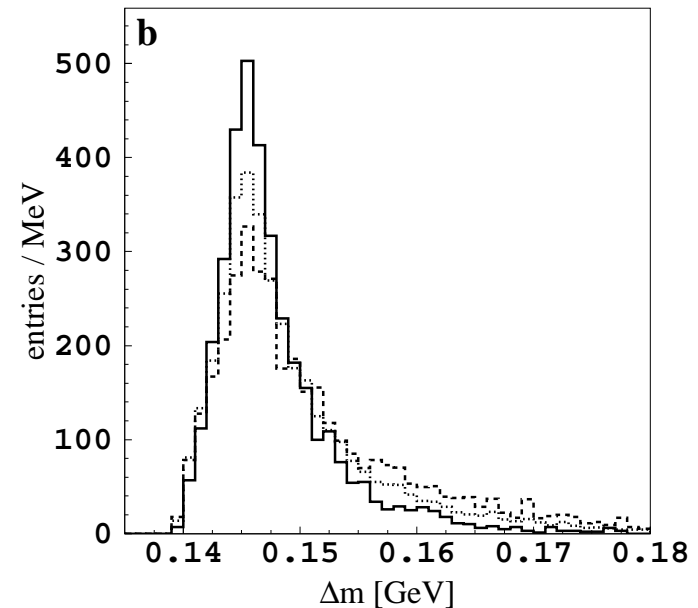
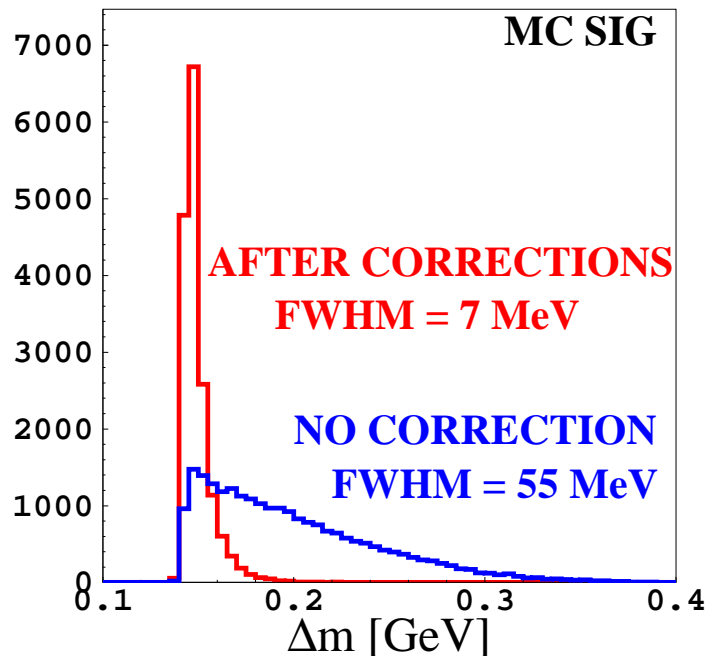
- simpler analysis, with no irreducible background

*but* no  $\sqrt{R_D y'}$  term to increase rate

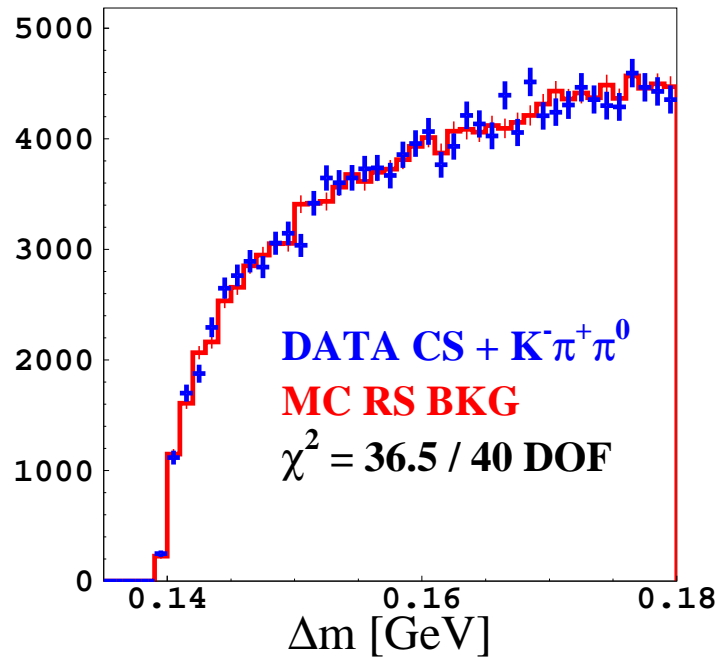
*and*  $\nu \rightarrow$  lost information: background  $N_B \propto \frac{dN_B}{dQ} \cdot \sigma_Q$

- ⊙ use simple  $t$  cut to suppress background [traditional]
- ⊙ use constraints to improve  $\vec{\sigma}(\vec{p})$ , hence  $\sigma_Q$  [ $\sim$  new]

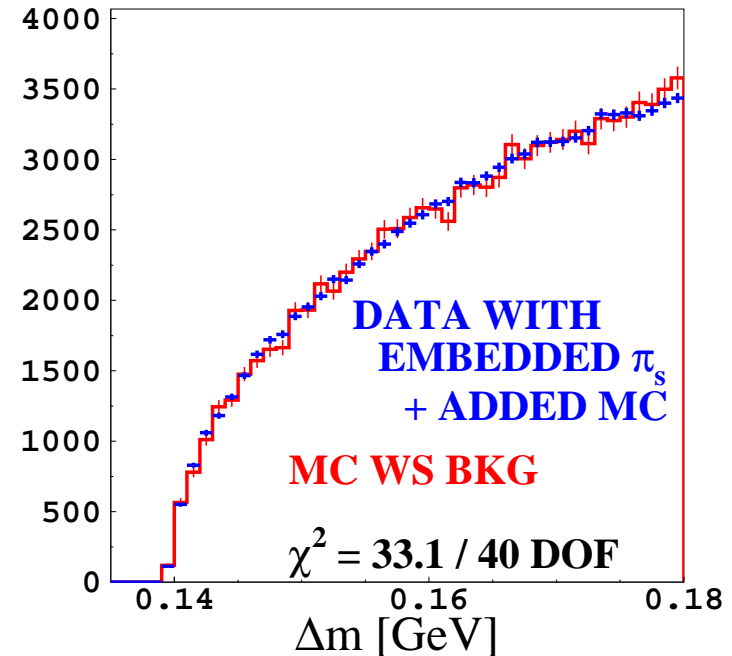
1. take naïve  $P_\nu = P_{\text{cms}} - P_{\pi K e} - P_{\text{rest}}$
2. require  $-4 \text{ GeV}^2/c^4 < M(\pi K e \nu)^2 < 36 \text{ GeV}^2/c^4$
3. rescale  $P_{\text{rest}}$ :  $M(\pi K e \nu)^2 = (P_{\text{cms}} - x \cdot P_{\text{rest}})^2 \equiv m_{D^*}$
4. require  $-2 \text{ GeV}^2/c^4 < P_\nu^2 < 0.5 \text{ GeV}^2/c^4$
5. rotate  $\vec{p}_{\text{rest}}$ :  $m_\nu^2 = (E_{\text{cms}} - E_{\pi K e} - E_{\text{rest}})^2 - p_{\pi K e}^2 - p_{\text{rest}}^2 - 2p_{\pi K e} p_{\text{rest}} \cos \alpha \equiv 0$



- suppress photon conversions, serious when  $e^+e^- \xrightarrow{\text{ID}} \pi_{\text{slow}}^+ e^-$ :  
 $M(e^+e^-) > 150 \text{ MeV}/c^2 \quad \forall$  combinations with  $\pi_{\text{slow}}^+$  or  $e^-$
- model backgrounds using **data**, with **MC corrections**:  
 right sign: wrong sign:

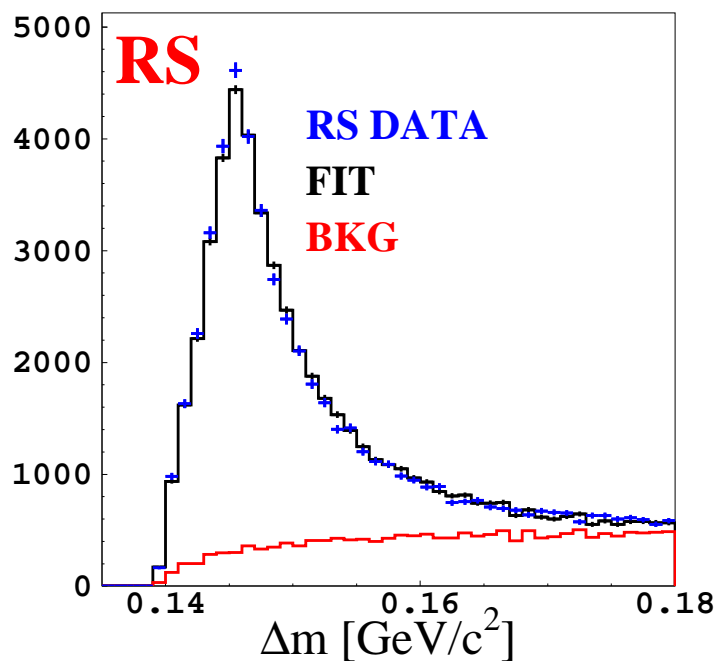


“combinatorial sign”  $K^\pm e^\pm$   
 + MC charge-correlated:  $K^- \pi^+ \pi^0$



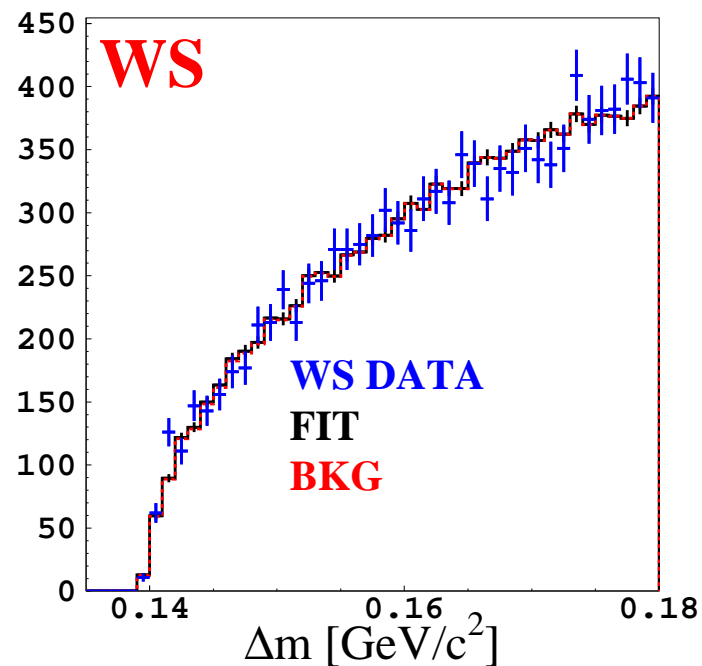
event mixing for (un)correlated bkgd  
 + MC ang-correlated:  $K^- \pi^+ \pi^0$

right sign:



$$N_{RS} = 40198 \pm 329$$

wrong sign:



$$N_{WS} = 19 \pm 67$$

$$r_D = (0.20 \pm 0.70 \pm 0.11) \times 10^{-3}$$

$$< 1.4 \times 10^{-3} \text{ @ 90\% CL}$$



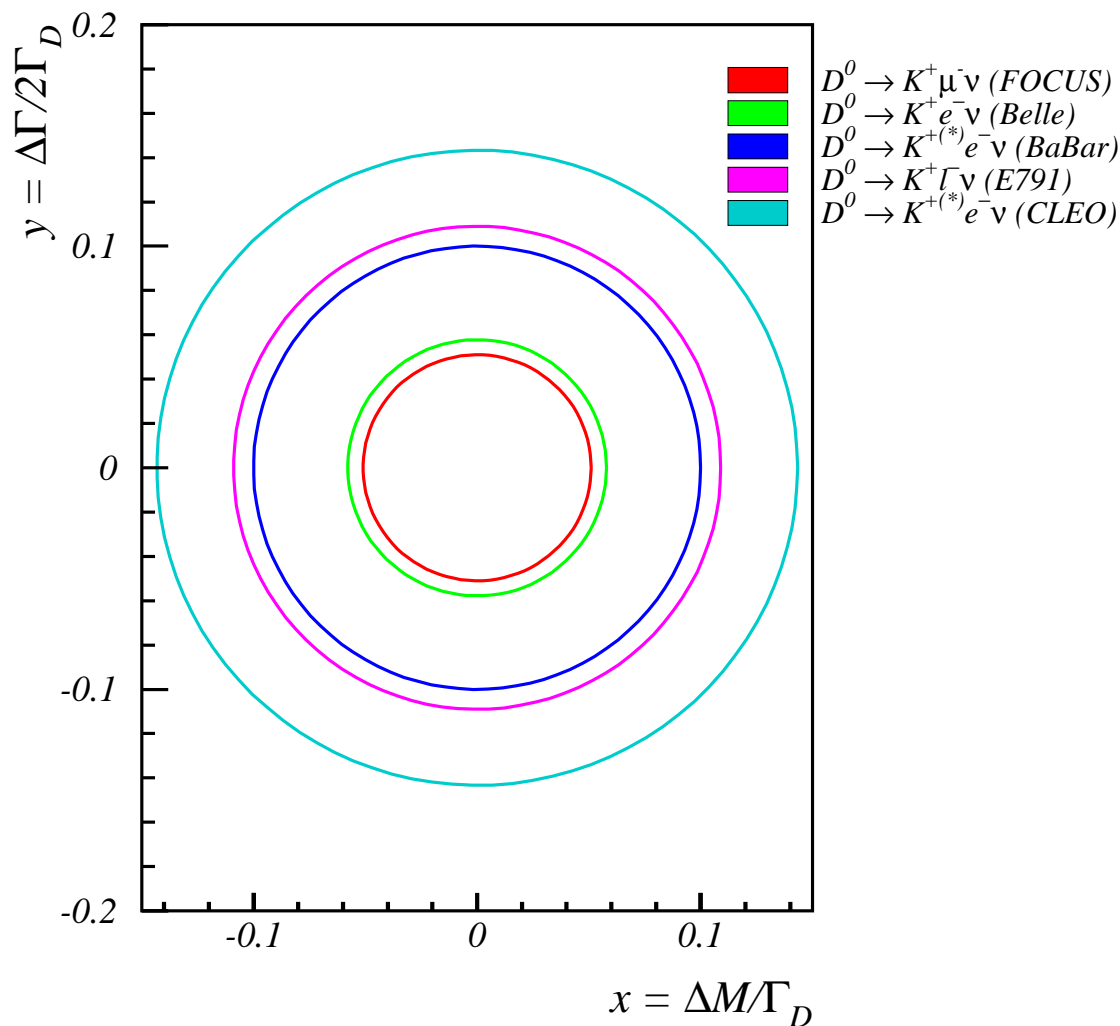
# $D^0-\bar{D}^0$ mixing summary (semileptonic)



From G. Burdman and I. Shipsey, arXiv:hep-ph/0310076, updated 20-Aug-2004:

[arXiv:hep-ex/0408112](http://arxiv.org/abs/hep-ex/0408112)

- most restrictive save the FOCUS thesis (unpublished 2002)
- extending:  $2\times$  data
- adding  $K^+\mu^-\bar{\nu}_\mu$
- $\rightarrow$  PRD this year
- cf. the reach of ...





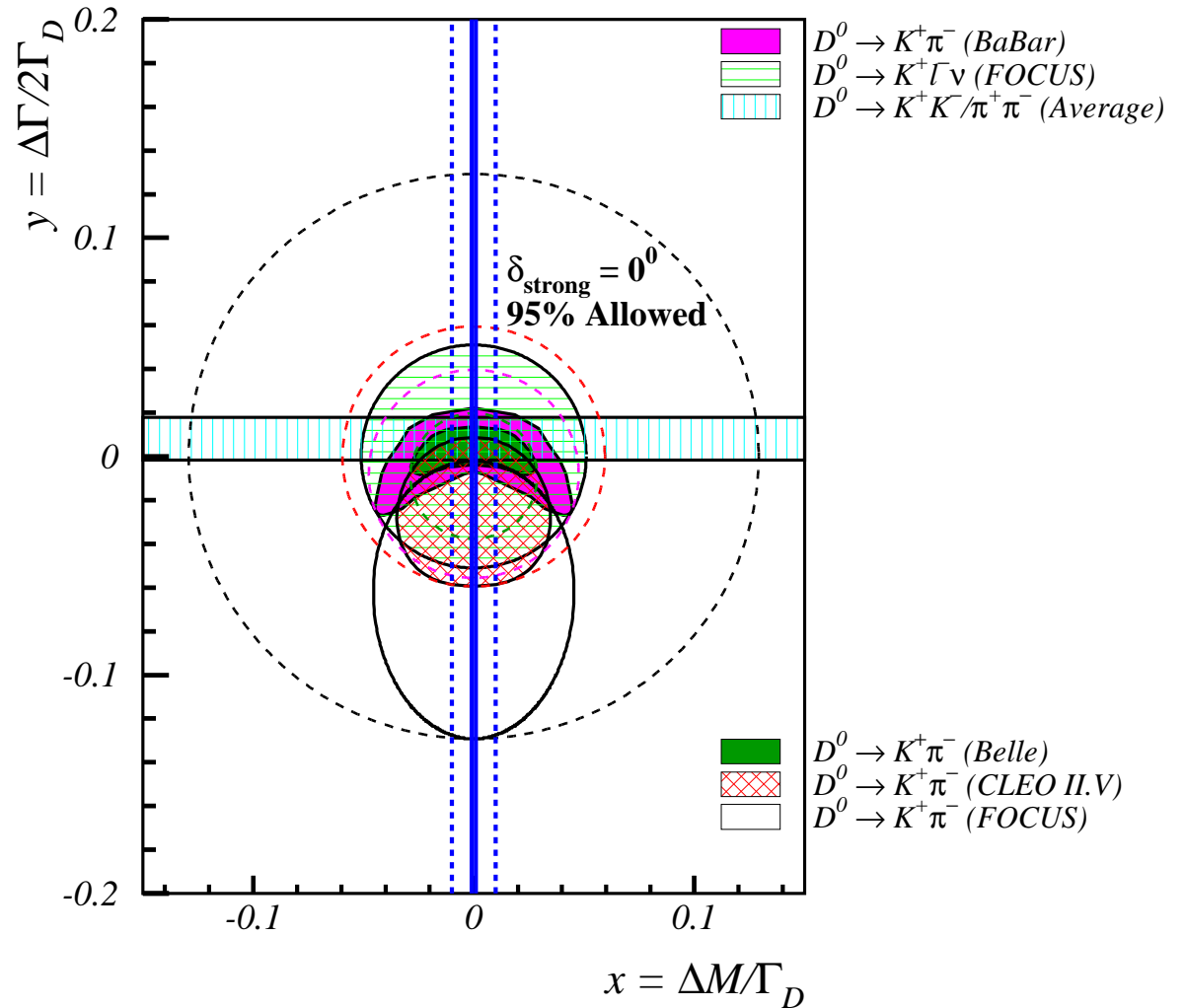
# $D^0-\bar{D}^0$ mixing summary (all)



From G. Burdman and I. Shipsey, arXiv:hep-ph/0310076, updated 20-Aug-2004:

[arXiv:hep-ex/0408125](http://arxiv.org/abs/hep-ex/0408125)

- most restrictive single result
- $\rightarrow$  PRL now
- cf.  $y_{CP}$  ...
- note  $\delta_{K\pi}$  unknown
- reached % level





# BACKUP SLIDES

---



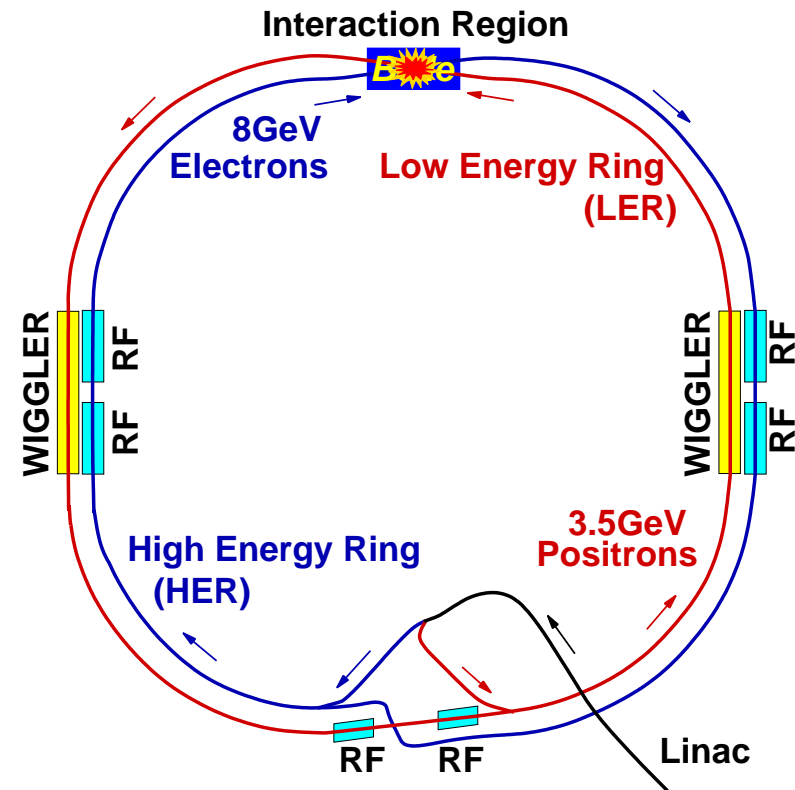
# The Belle Collaboration

*~400 physicists from 13 regions, 59 institutions*



The “KEKB” asymmetric energy  $e^+e^-$  collider:

- 3.5 GeV  $e^+$  on 8.0 GeV  $e^-$
- $\sqrt{s} = 10.58 \text{ GeV} \equiv M(\Upsilon(4S))$
- continuous injection
- peak performance:
  - $1.39 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$   
=  $14 \text{ nb}^{-1} \text{ s}^{-1}$
  - $944 \text{ pb}^{-1}/\text{day}$
- cf.  $\sigma_{\Upsilon(4S)} \approx 1 \text{ nb}$ ,  $\sigma_{c\bar{c}} \approx 1.3 \text{ nb}$
- $\int dt \mathcal{L} > 287 \text{ fb}^{-1}$



single collision point instrumented with ...

$e^+e^-$  at  $\sqrt{s} = 10.58 \text{ GeV}$ :  $90 \text{ fb}^{-1}$  ( $K^+\pi^-$ ),  $140 \text{ fb}^{-1}$  ( $K^+e^-\bar{\nu}_e$ )

- 1.5 T solenoid
- 3-layer SVD, 50-layer CDC

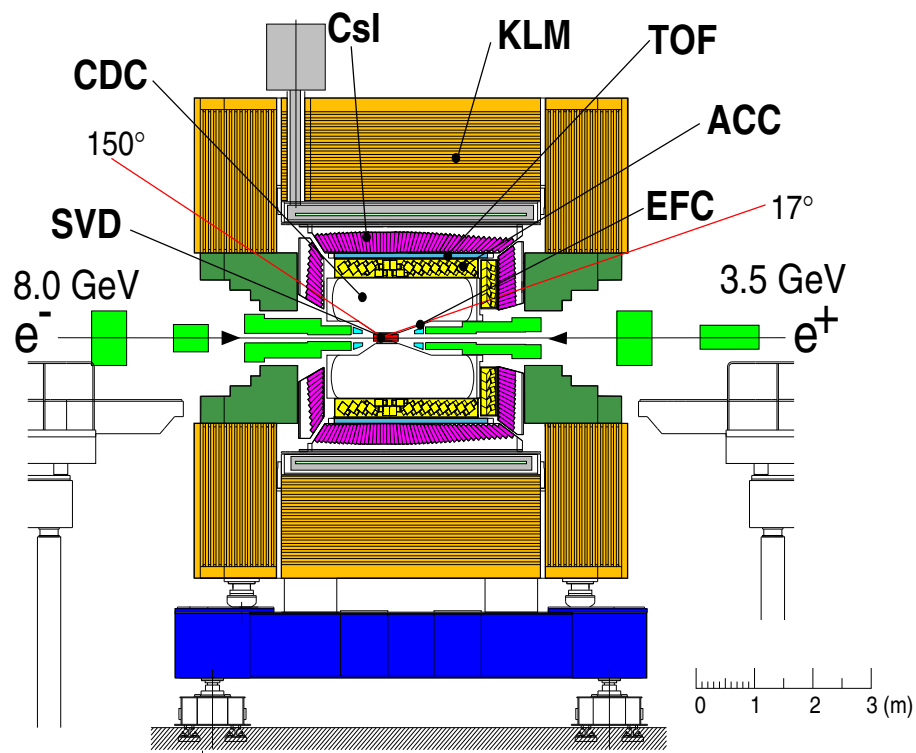
- $\frac{\sigma_{p_T}}{p_T} = (0.19p_T \oplus 0.3)\%$

- $\sigma_{xy} = \left(19 \oplus \frac{49}{p\beta \sin^{3/2}\theta}\right) \mu\text{m}$

- $\sigma_z = \left(28 \oplus \frac{41}{p\beta \sin^{5/2}\theta}\right) \mu\text{m}$

- $\frac{\sigma_E}{E} = \left(1.3 \oplus \frac{0.07}{E} \oplus \frac{0.8}{E^{1/4}}\right) \%$

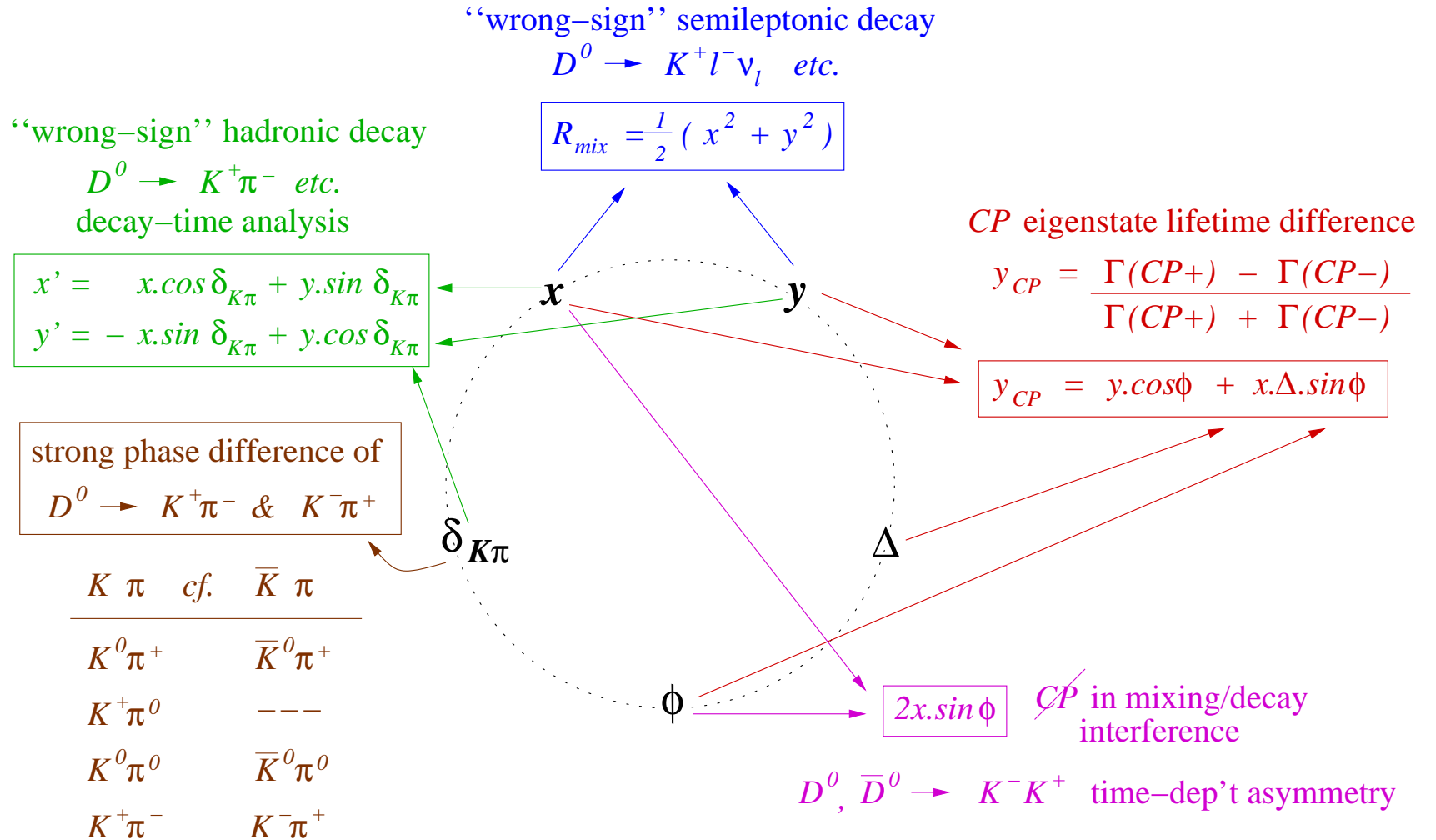
- PID:  $\left\{ \begin{array}{l} \sigma_{dE/dx} = 6.9\% \\ \sigma_{TOF} = 95 \text{ ps} \\ \text{aerogel Čerenkov} \end{array} \right.$



+ ECAL,  $dE/dx$  etc. for  $e^\pm$  ID ...

+ the KLM ( $K_L^0$  and  $\mu$  system) ...

$\epsilon(K^\pm) \approx 85\% \text{ for } \pi^\pm \text{ fake-rate } \lesssim 10\% \text{ up to } 3.5 \text{ GeV}/c$



MC right-sign backgrounds (cf. wrong-sign breakdown)

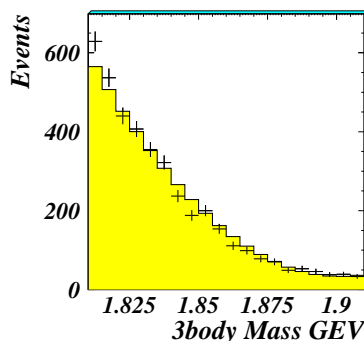
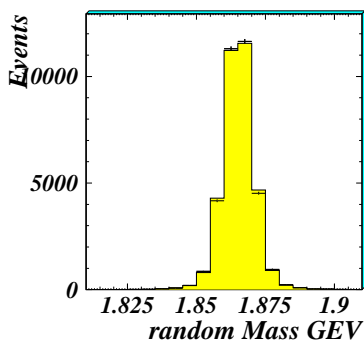
“random  $\pi_{\text{slow}}$ ”

$D^0$  3-body

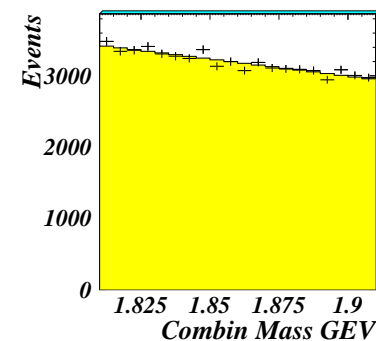
$D^+, D_s^+$

combinatorial

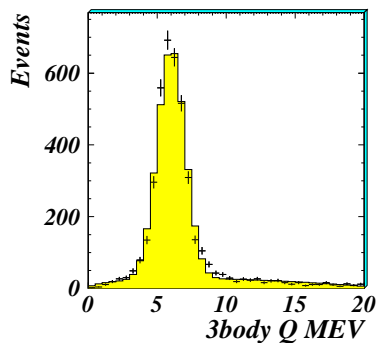
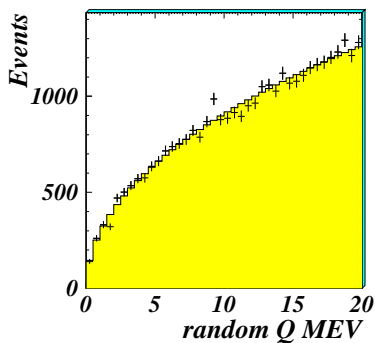
$M$



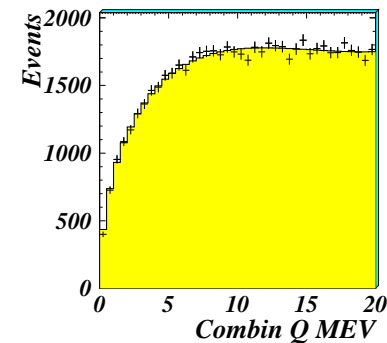
[negligible]



$Q$



[negligible]



negligible  $D^+, D_s^+$  background in this case



# $D^0 \rightarrow K^+ \pi^-$ : timing distributions & resolution



bkgd:	random $\pi_{\text{slow}}$	$D^0$ 3-body	$D^+, D_s^+$	comb <sup>l</sup>
$f_i(t)$	$\exp(-t/\tau_{D^0})$	$\exp(-t/\tau_{D3b})$	$\exp(-t/\tau_{Dch})$	$\delta(t)$
$\tau$ param.	PDG	sideband	MC	—
resolution	$\mathcal{R}_{\text{signal}}$	$\mathcal{R}_{\text{signal}}$	$\mathcal{R}_{\text{signal}}$	$\mathcal{R}_{\text{comb}}$

$$\mathcal{R}(t_i, t'; \sigma_{t,i}) = (1 - f_{\text{tail}})\mathcal{G}(t_i - t'; \mu, S\sigma_{t,i}) + f_{\text{tail}}\mathcal{G}(t_i - t'; \mu, S_{\text{tail}}\sigma_{t,i})$$

Beginning with a simplified background model,

- fit 1: RS signal region  $\longrightarrow$  provisional  $\mathcal{R}_{\text{signal}}$  parameters
- fit 2: RS sideband region  $\longrightarrow$   $\mathcal{R}_{\text{comb}}$  parameters &  $\tau_{D3b}$  for RS
- fit 3: RS signal region  $\longrightarrow$   $\mathcal{R}_{\text{signal}}$  parameters;  $\tau_{D^0}$  as check
- fit 4: WS sideband region  $\longrightarrow$   $\mathcal{R}_{\text{comb}}$  parameters &  $\tau_{D3b}$  for WS
- fit 5: WS signal region  $\longrightarrow$  FINAL RESULT



# $D^0 \rightarrow K^+ \pi^-$ : CPV parametrization



- $A_D = (R_D^+ - R_D^-)/(R_D^+ + R_D^-)$ : CPV in DCS decay
- $A_M = (R_M^+ - R_M^-)/(R_M^+ + R_M^-)$ : CPV in  $D^0$ - $\bar{D}^0$  mixing  
where  $R_M^\pm = 0.5(x'^{\pm 2} + y'^{\pm 2})$
- $\phi$  (weak phase): CPV in interference of DCS/mixed amplitudes

$$x'^{\pm} = \left[ \frac{1 \pm A_M}{1 \mp A_M} \right]^{\frac{1}{4}} (x' \cos \phi \pm y' \sin \phi)$$
$$y'^{\pm} = \left[ \frac{1 \pm A_M}{1 \mp A_M} \right]^{\frac{1}{4}} (y' \cos \phi \mp x' \sin \phi)$$

convention-independent set  $(x' \sin \phi, y' \cos \phi, (x'^2 + y'^2))$   
also suggested in the literature



For points  $\vec{\alpha} = (x'^2, y')$

- generate ensemble of toy MC datasets  $\{X_i\}_j$
- $\forall j$ , fit the dataset  $\{X_i\}$  and
  - record  $\Delta\ell_j = \ln \mathcal{L}_j^{\max} - \ln \mathcal{L}_j(\vec{\alpha})$
  - compare with  $\Delta\ell_{\text{data}} = \ln \mathcal{L}_{\text{data}}^{\max} - \ln \mathcal{L}_{\text{data}}(\vec{\alpha})$
- do 95% of the  $\{X_i\}_j$  have  $\Delta\ell_j < \Delta\ell_{\text{data}}$ ??
  - if yes, this  $\alpha$  is on the contour
  - if no, choose another  $\alpha$  [a search strategy is used]

The resulting contour implements [likelihood-ratio ordering](#) (Feldman-Cousins) without having to generate ensembles  $\forall \alpha$

Taken from B.Aubert *et al.* (BaBar), *Phys. Rev. Lett.* **91**, 171801 (2003).